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**FORTRAN SIN**  
**A One-Dimensional Hydrodynamic Code**  
**for Problems Which Include Chemical Reactions,**  
**Elastic-Plastic Flow, Spalling, and Phase Transitions**



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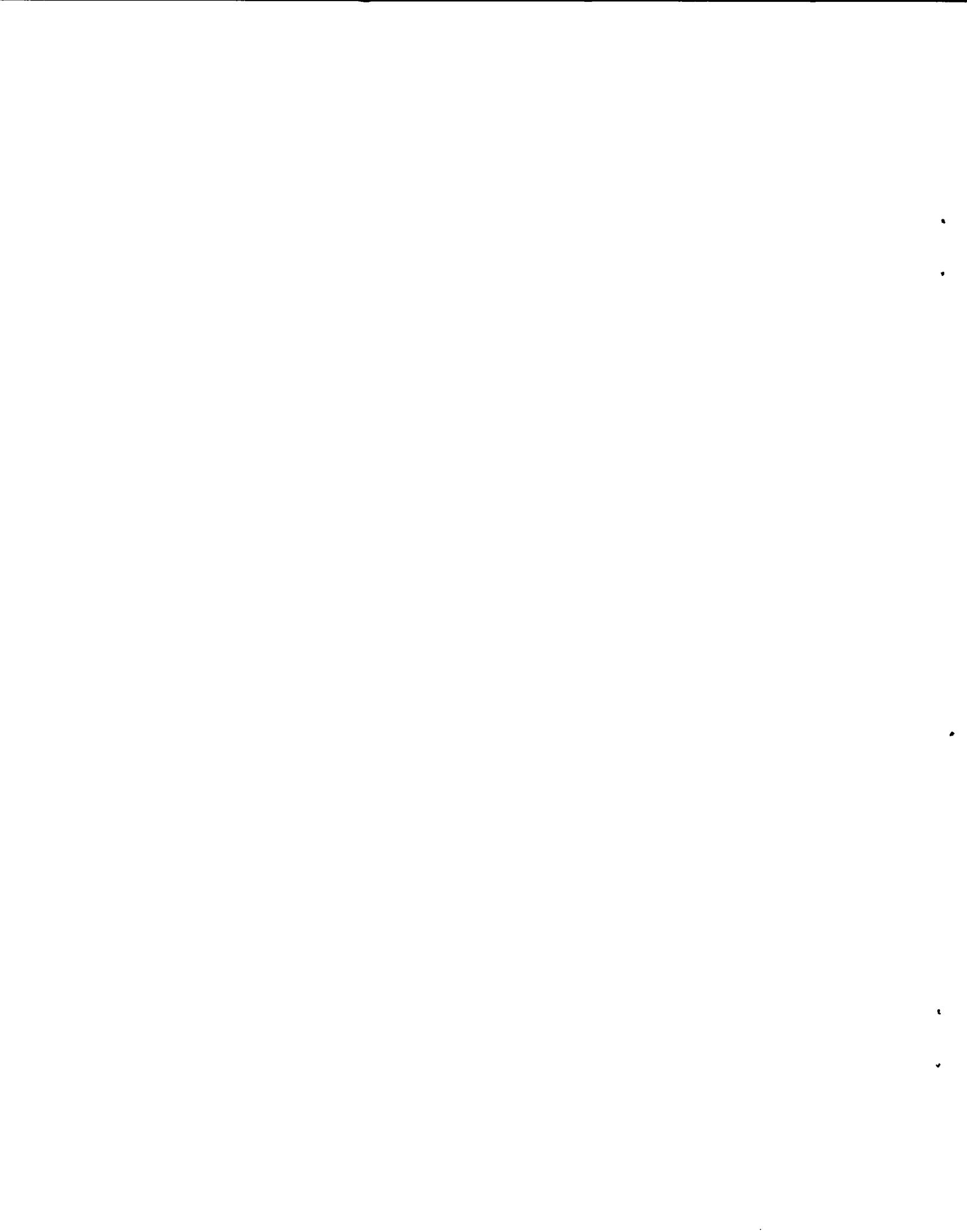
**FORTRAN SIN**  
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by

Charles L. Mader

William R. Gage





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FORTRAN SIN: A ONE-DIMENSIONAL HYDRODYNAMIC CODE FOR PROBLEMS WHICH INCLUDE  
CHEMICAL REACTIONS, ELASTIC-PLASTIC FLOW, SPALLING, AND PHASE TRANSITIONS

by

Charles L. Mader and William R. Gage

ABSTRACT

This report describes a CDC 6600 computer FORTRAN code for computing one-dimensional hydrodynamic problems in slab, cylindrical, or spherical geometry using realistic equations of state. Features available in the code include chemical reaction using an Arrhenius rate law, the C-J volume burn, or, for slabs, a gamma-law Taylor wave; elastic-plastic flow using the Hooke's law-Von Mises yield model; and spalling using the Whiteman and Skidmore model of the tensile stress at spalling as a linear function of the square root of the stress rate. The HOM equation of state is used to compute the equation of state for detonation products, undecomposed explosives, mixtures of the two, and condensed components which may have an instantaneous phase change.

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I. INTRODUCTION

The SIN technique for solving reactive one-dimensional problems has been a useful research tool for almost ten years. The first version was written in machine language for the IBM 7090.<sup>1</sup> The second version was written in machine language for the IBM 7030 (STRETCH) and is called STRETCH SIN.<sup>2</sup> Because of its detailed treatment of the equation of state and its ability to compute the detailed structure of complicated reactive and nonreactive hydrodynamic problems, SIN has been used to study other interesting engineering and research problems. The new numerical techniques which resulted from these studies have been included in this new version of SIN, written in FORTRAN IV language for the CDC 6600 and called FORTRAN SIN.

The code includes the effects of heat conduction, viscosity, elastic-plastic flow, spalling, and reactive flow. As presented in this report, the code can handle 10 components and 999 mesh points; however, these limits can be increased several times

without exceeding the core memory of the CDC 6600 or IBM 7030. The boundary conditions may be continuous, a free surface, a piston with a constant, a linearly varying velocity, or, for slabs, a reactive steady-state velocity.<sup>3</sup> The PIC or Landshoff forms for the artificial viscosity may be used, and a form for real viscosity in slab geometry is available.

The HOM equation of state is used. One may compute the equation of state of condensed explosives, detonation products, and mixtures of the two. The equation of state for the condensed component may include an instantaneous phase change such as that described for iron.<sup>4</sup>

The code includes the Hooke's law-Von Mises model for elastic-plastic flow as described for aluminum.<sup>5</sup> It also includes spalling, using the Whiteman and Skidmore model of the tensile stress at spalling as a linear function of the square root of the tensile stress.<sup>6,7</sup> It permits chemical reaction using an Arrhenius rate law, the C-J volume burn, or, for

slabs, a gamma-law Taylor wave.

The code includes features permitting microfilm listings and graphs of pressure, temperature, mass fraction, density, and particle velocity vs. Eulerian radius. Tape dumps are taken at input intervals of the cycle number, and the problem may be restarted from any desired tape dump. Problems with pistons may use the variable number of cells feature for a considerable reduction of running time.

The SIN code has been written not as a special purpose production code but as a general purpose research and engineering tool. It will continue to change (hopefully for the better) as new developments in the numerical description of real materials under high impulse become available.

This report describes the numerical methods of SIN in complete detail. It also presents sufficient details to enable a coder to follow and change the code. The latter information is not of interest to the casual reader.

## II. THE FLOW EQUATIONS

### The Nomenclature

|          |   |
|----------|---|
| $D_{CJ}$ | the C-J detonation velocity                           |
| $E$      | total energy (Mbar-cc/g)                              |
| $E^*$    | activation energy                                     |
| $I$      | internal energy (Mbar-cc/g)                           |
| $j$      | net point of the Lagrangian mesh                      |
| $K$      | a constant of about 2 or the coefficient of viscosity |
| $M$      | mass  |
| $n$      | time cycle  |
| $P$      | pressure (Mbar)                                       |
| $q$      | artificial viscosity                                  |
| $R$      | Eulerian radius                                       |
| $r$      | Lagrangian radius                                     |
| $S_x$    | elastic stress deviator in x or r direction           |
| $S_z$    | elastic stress deviator in z direction                |
| $T$      | temperature ( $^{\circ}$ K)                           |
| $U$      | particle velocity (cm/ $\mu$ sec)                     |
| $V$      | specific volume (cc/g)                                |
| $V_{CJ}$ | the C-J volume of the detonation products             |

|              |   |
|--------------|---|
| $W$          | mass fraction of undecomposed explosive   |
| $Y_0$        | yield strength  |
| $Z$          | frequency factor  |
| $\alpha$     | =1 for slabs, =2 for cylinders, =3 for spheres  |
| $\gamma$     | $\gamma$ -law gas constant since $\ln P = A + \gamma \ln V$ , $\gamma = B$ in HOM equation of state subroutine. |
| $\Delta t$   | time ( $\mu$ sec)   |
| $\lambda$    | thermal conductivity coefficient  |
| $\mu$        | shear modulus   |
| $\rho$       | = 1/V   |
| $\rho_0$     | $1/V_0$ where $V_0$ is initial specific volume  |
| $(\rho_0)_i$ | initial density for the i <sup>th</sup> component (g/cc)  |

### The Differential Equations

The Lagrangian conservation equations in one dimension for slabs, cylinders, and spheres are:

$$\frac{\partial U}{\partial t} = -R^{\alpha-1} \frac{\partial \sigma}{\partial M} - (\alpha-1) \frac{V\varphi}{R} \quad \text{Conservation of momentum,}$$

$$V = R^{\alpha-1} \frac{\partial R}{\partial M} \quad \text{Conservation of mass,}$$

and

$$\frac{\partial E}{\partial t} = -\frac{\partial \sigma U R^{\alpha-1}}{\partial M} + \lambda \frac{\partial}{\partial M} \left( R^{\alpha-1} \frac{\partial T}{\partial R} \right) \quad \text{Conservation of energy with heat conduction term,}$$

where  $E = I + 0.5U^2$ .

$$\frac{\partial R}{\partial t} = U,$$

and

$$dM = \rho_0 r^{\alpha-1} dr = \rho R^{\alpha-1} dR,$$

where  $dM$  is element of mass per unit of solid angle ( $\alpha=2$  or  $3$ ) or of surface ( $\alpha=1$ ).  $\sigma$  is the sum of the viscous pressure, the equation of state pressure, and the stress deviator,  $S_x$ .  $\varphi = 2S_x + S_z$ , which for spherical geometry is  $3/2 S_x$  since  $S_z = -1/2 S_x$ .

$$\frac{\partial S_x}{\partial t} = 2\mu \left( -\frac{\partial U}{\partial R} + \frac{1}{3V} \frac{\partial V}{\partial t} \right).$$

$$\frac{\partial S_z}{\partial t} = + \frac{2}{3} \left( \frac{\mu}{V} \frac{\partial V}{\partial t} \right).$$

In this report we use the convention that the stress deviators have the same sign as pressure; that is, positive in compression and negative in tension. This convention is the reverse of that used by most workers in the field.

#### The Difference Equations

The difference equations presented below are discussed in References 1 and 5. The pressure, temperature, energy, specific volume, and mass fraction of the cells are considered to be located at the centers of mass of the elements, and the particle velocity is considered to be located at the boundary between the cells.

#### A. The Initial Conditions

$$R_{j+\frac{1}{2}} = \sum_{i=1}^j (\Delta R)_i,$$

where  $j = 1, 2, \dots$ , and the  $i$ th component is located between  $j$  and  $j+k$  where  $k$  is the number of cells for each component.

$$M_j = (o_o)_i \left[ \left( R_{j-\frac{1}{2}} + R_{j+\frac{1}{2}} \right)^{1/2} \right]^{\alpha-1} (\Delta R)_i.$$

#### B. The Conservation Equations for Time Advancement

##### 1. Subroutine VELOC (NMIN,NMAX)

$$U_{j+\frac{1}{2}}^{n+\frac{1}{2}} = U_{j+\frac{1}{2}}^{n-\frac{1}{2}} + \frac{(\Delta t) \left( R_{j+\frac{1}{2}}^n \right)^{\alpha-1}}{0.5(M_j + M_{j+1})} \left[ \left( P_j^n - P_{j+1}^n \right) + \left( q_j^n - q_{j+1}^n \right) \right] - \frac{(\alpha-1)}{2} \frac{(\varphi) \left( V_j^n + V_{j+1}^n \right) (\Delta t)}{R_{j+\frac{1}{2}}^n},$$

where

$$\varphi = \frac{3}{4} \left( Sx_j^n + Sx_{j+1}^n \right) \quad \text{for } \alpha = 3,$$

and

$$v = \frac{1}{2} \left[ 2 \left( Sx_j^n + Sx_{j+1}^n \right) + \left( Sz_j^n + Sz_{j+1}^n \right) \right]$$

for  $\alpha = 2$ .

##### 2. Subroutine RADIUS (NMIN,NMAX)

$$R_{j+\frac{1}{2}}^{n+1} = R_{j+\frac{1}{2}}^n + U_{j+\frac{1}{2}}^{n+\frac{1}{2}} (\Delta t). \quad (1)$$

##### 3. Subroutine VOLUM (NMIN,NMAX)

$$V_j^{n+1} = \left( \frac{R_{j-\frac{1}{2}}^{n+1} + R_{j+\frac{1}{2}}^{n+1}}{2} \right)^{\alpha-1} \left( \frac{R_{j+\frac{1}{2}}^{n+1} - R_{j-\frac{1}{2}}^{n+1}}{M_j} \right).$$

##### 4. Subroutine ENERGY (NMIN,NMAX)

$$I_j^{n+1} = I_j^n + \frac{(\Delta t)}{M_j} \left\{ \left[ \frac{M_j P_{j-1}^n + M_{j-1} P_j^n}{M_j + M_{j-1}} + 0.5(q_j^n + q_{j-1}^n) \right] \right.$$

$$U_{j-\frac{1}{2}}^{n+\frac{1}{2}} \left( R_{j-\frac{1}{2}}^{n+1} \right)^{\alpha-1} - \left[ \frac{M_{j+1} P_j^n + M_j P_{j+1}^n}{M_j + M_{j+1}} + 0.5(q_j^n + q_{j+1}^n) \right]$$

$$U_{j+\frac{1}{2}}^{n+\frac{1}{2}} \left( R_{j+\frac{1}{2}}^{n+1} \right)^{\alpha-1} \left\} + \frac{1}{8} \left[ \left( U_{j+\frac{1}{2}}^{n-\frac{1}{2}} + U_{j-\frac{1}{2}}^{n-\frac{1}{2}} \right)^2 - \left( U_{j+\frac{1}{2}}^{n+\frac{1}{2}} + U_{j-\frac{1}{2}}^{n+\frac{1}{2}} \right)^2 \right].$$

##### 5. Subroutine HETCON (NMIN,NMAX)

$$T_j^{n+1} = T_j^n + \frac{\lambda(\Delta t)}{M_j} \left[ \left( \frac{R_{j+\frac{1}{2}}^{n+1}}{R_{j+\frac{1}{2}}^{n+1} - R_{j-\frac{1}{2}}^{n+1}} \right)^{\alpha-1} \left( T_{j+1}^n - T_j^n \right) \right. \\ \left. - \left( \frac{R_{j-\frac{1}{2}}^{n+1}}{R_{j+\frac{1}{2}}^{n+1} - R_{j-\frac{1}{2}}^{n+1}} \right)^{\alpha-1} \left( T_j^n - T_{j-1}^n \right) \right].$$

#### C. Viscosity - Subroutine VISCOS (NMIN,NMAX)

##### 1. PIC Form

$$q_j^{n+1} = \frac{K}{V_j^{n+1}} (0.5) \left( U_{j-\frac{1}{2}}^{n+\frac{1}{2}} + U_{j+\frac{1}{2}}^{n+\frac{1}{2}} \right) \left( U_{j-\frac{1}{2}}^{n+\frac{1}{2}} - U_{j+\frac{1}{2}}^{n+\frac{1}{2}} \right),$$

if  $\left( U_{j-\frac{1}{2}}^{n+\frac{1}{2}} - U_{j+\frac{1}{2}}^{n+\frac{1}{2}} \right)$  is positive; otherwise,  $q_j^{n+1} = 0$ .

The absolute value of  $q$  is used.

##### 2. Landshoff Form

$$q_j^{n+1} = \frac{K}{V_j^{n+1}} \left( U_{j-\frac{1}{2}}^{n+\frac{1}{2}} - U_{j+\frac{1}{2}}^{n+\frac{1}{2}} \right).$$

Restrictive conditions are the same as for the PIC form.

##### 3. "Real" Form

$$q_j^{n+1} = 1.333 \frac{K}{V_j^{n+1}} \frac{\left( U_{j-\frac{1}{2}}^{n+\frac{1}{2}} - U_{j+\frac{1}{2}}^{n+\frac{1}{2}} \right)}{M_j},$$

where  $K$  is the "coefficient of viscosity," and this form is appropriate only for slabs.

D. Burn Techniques - Subroutine BURN (NMIN,NMAX)

for 1 and 2

1. Arrhenius Burn

$$w_j^{n+1} = w_j^n - \Delta t Z w_j^n e^{-E^*/R_g T_j^n}$$

where  $1 \geq w \geq 0$ .

2. C-J Volume Burn

Assumes that  $w$  varies linearly with  $V$  from  $v_o$  to  $v_{CJ}$ .

$$w_j^{n+1} = 1 - \frac{v_o - v_j^{n+1}}{v_o - v_{CJ}}$$

where

$$1 \geq w_j^{n+1} \geq 0,$$

and

$$w_j^n \geq w_j^{n+1}.$$

$$P_j^{n+1} = (1 - w_j^{n+1}) (P^1)$$

where  $P^1$  is pressure of detonation products at  $V$ ,  $I$ , and  $w = 0$ , if  $w_j^{n+1} < 0.99$  (WMAX); otherwise,  $P_j^{n+1} = P_o$ . The  $P_j^{n+1}$  calculation is actually performed in the subroutine EQST.

3. Gamma-Law Taylor Wave Burn

The explosive is burned before the first time interval by assuming it to be a gamma-law explosive that has been detonated with a rear boundary of constant velocity. Coded as part of initial setup.

Knowing  $a_o$ ,  $\gamma$ ,  $D_{CJ}$ , we compute

$$U_{CJ} = \frac{D_{CJ}}{\gamma + 1}$$

$$P_{CJ} = \frac{\rho_o D_{CJ}^2}{\gamma + 1}$$

$$V_{CJ} = \left( \frac{\gamma}{\gamma + 1} \right) \left( \frac{1}{\rho_o} \right)$$

$$C_{CJ} = D_{CJ} - U_{CJ}$$

$$k = \frac{\gamma - 1}{\gamma + 1}$$

$$\ell = U_{CJ} - \frac{2}{\gamma - 1} C_{CJ}$$

and

$$t = \frac{R_n - R_o}{D_{CJ}}$$

where  $R_n - R_o$  is thickness of explosive.

For each cell with a radius of  $R_{j-\frac{1}{2}}$ , we compute

$$Y = \left( R_n - R_{j-\frac{1}{2}} \right) / t$$

$$U_{j+\frac{1}{2}} = \frac{2}{\gamma + 1} Y + k\ell$$

$$C_j = \frac{Y - 1}{2} (U_{j+\frac{1}{2}} - \ell)$$

$$P_j = P_{CJ} \left( \frac{C_j}{C_{CJ}} \right)^{2\gamma/\gamma-1}$$

$$V_j = \left[ \frac{[P_{CJ}(V_{CJ})^\gamma]}{P_j} \right]^{1/\gamma}$$

$$I_j = \frac{P_j V_j}{\gamma - 1} - \frac{P_{CJ} V_{CJ}}{\gamma - 1} + \frac{P_{CJ}}{2} (v_o - v_{CJ})$$

and

$$R_{j+\frac{1}{2}} = R_{j-\frac{1}{2}} + (M_j)(V_j).$$

With the new  $R_{j+\frac{1}{2}}$  set equal to  $R_{j-\frac{1}{2}}$ , we return to compute  $Y$ , etc. When  $U_{j+\frac{1}{2}}$  is equal to the applied piston velocity, the rest of the explosive cells are made identical to the last cell calculated.

E. The Elastic Stress Deviators - Subroutine STRESS (NMIN,NMAX)

$$Sx_j^{n+1} = Sx_j^n + 2\mu \left[ - \left( \frac{U_{j+\frac{1}{2}}^{n+1} - U_{j-\frac{1}{2}}^{n+1}}{R_{j+\frac{1}{2}}^{n+1} - R_{j-\frac{1}{2}}^{n+1}} \right) (\Delta t) + \frac{2}{3} \left( \frac{V_j^{n+1} - V_j^n}{V_j^{n+1} + V_j^n} \right) \right].$$

$$Sz_j^{n+1} = Sz_j^n + \frac{4}{3}\mu \left( \frac{V_j^{n+1} - V_j^n}{V_j^{n+1} + V_j^n} \right).$$

F. The Equation of State and Yield Calculation - Subroutine EQST (NMIN,NMAX)

Enter HOM Subroutine with  $V_j^{n+1}$ ,  $I_j^{n+1}$ ,  $w_j^{n+1}$  to find  $P_j^{n+1}$ .

If  $P_j^{n+1} > P_o$ ,  
then

$$(P_{hyd})_j^{n+1} = (P_{hydrostat})_j^{n+1} = P_j^{n+1} - (2/3 Y_o) \left( \frac{P_j^{n+1}}{0.050} \right)$$

where

$$\frac{P_j^{n+1}}{0.050} \leq 1.0.$$

The 0.050 is input PLAP. If  $P_j^{n+1} < P_o$ , then

$$(P_{hyd})_j^{n+1} = P_j^{n+1}.$$

For  $\alpha = 1$  or 3 if

$$|Sx_j^{n+1}| \geq |2/3 Y_o|, P_j^{n+1} = (P_{hyd})_j^{n+1} + 2/3 Y_o$$

where the sign of  $(2/3 Y_o)$  is identical to the sign of  $Sx_j^{n+1}$ . Or if

$$|Sx_j^{n+1}| < |2/3 Y_o|, P_j^{n+1} = (P_{hyd})_j^{n+1} + Sx_j^{n+1}.$$

For  $\alpha = 2$

$$f = 2 \left[ (Sx_j^{n+1})^2 + Sx_j^{n+1} Sz_j^{n+1} + (Sz_j^{n+1})^2 \right].$$

Then if

$$f < 2/3 (Y_o)^2, P_j^{n+1} = (P_{hyd})_j^{n+1} + Sx_j^{n+1},$$

and

$$Sz_j^{n+1} = Sz_j^{n+1}.$$

Or if

$$f > 2/3 (Y_o)^2, P_j^{n+1} = (P_{hyd})_j^{n+1} + \left( \sqrt{\frac{2/3 (Y_o)^2}{f}} \right) (Sx_j^{n+1}),$$

and

$$Sz_j^{n+1} = (Sz_j^{n+1}) \left( \sqrt{\frac{2/3 (Y_o)^2}{f}} \right).$$

#### G. Total Energy of Components Coded as Part of Subroutine TIME

$$\text{Kinetic energy} = \sum_1^j \xi M_j \left( \frac{U_{j+\frac{1}{2}}^{n+1}}{(2)(0.9992768)} \right)^2$$

$$\text{Internal energy} = \sum_1^j \xi M_j \left( I_j^{n+1} \right),$$

where  $\xi = 4\pi$  for spheres,  $2\pi$  for cylinders, and 1 for slabs; and the units of energy are Mbar-cc/g.

#### H. The Boundary Conditions

##### 1. An Applied Piston on Right Boundary

$U_{j+\frac{1}{2}}^n = U_{\text{piston}}$  where outside boundary is  $j+\frac{1}{2}$ ,  
if  $W_{j-3}^n > 0.5$ ; otherwise = final  $U_{\text{piston}}$ , or  
 $U_{\text{piston}} = A + (B)(\text{Time})$ . For both,

$$P_{j+1}^n = P_j^n, \text{ and } Q_{j+1}^n = Q_j^n.$$

##### 2. An Applied Piston on Left Boundary

$U_{\frac{1}{2}}^n = U_{\frac{1}{2}}^{n+1} = U_{\text{piston}}$  where boundary is at  $j = \frac{1}{2}$   
if  $W_{j+3}^n > 0.5$ ; otherwise = final  $U_{\text{piston}}$ , or  
 $U_{\text{piston}} = A + (B)(\text{Time})$ . For both,

$$P_o^n = P_1^n, \text{ and } q_o^n = q_1^n.$$

$R_{\frac{1}{2}}$  is computed by Equation (1).

##### 3. A Steady-State Reaction Zone Piston on Left Boundary

The steady-state reaction zone piston is computed by iteration for a given detonation velocity by using the amount of reaction that occurred in a cell near the piston to determine the proper particle velocity of the piston.

For a W, iterate on V using linear feedback by calculating

$$I = I_o + \frac{1}{2} (o_o)^2 (D_{CJ})^2 (V_o - v)^2$$

and

$$P_r = P_o + (o_o)^2 (D_{CJ})^2 (V_o - v)$$

where  $P_r$  is Rayleigh line pressure.

Using the HOM equation of state, calculate P for V, I, and W. Continue iteration until  $P_r - P \leq 1 \times 10^{-5}$ . Calculate  $U = \sqrt{(P - P_o)(V_o - v)}$  and assign it to final  $U_{\text{piston}}$ .

##### 4. A Right Free-Surface Boundary

$$P_{j+1}^n = -P_j^n \text{ where outside boundary is } j+\frac{1}{2}.$$

$$U_{j+1}^n = U_j^n.$$

## 5. A Left Free-Surface Boundary

$$P_o^n = -P_1^n \text{ where boundary is at } j = \frac{1}{2}.$$

$$U_{\frac{1}{2}}^n = -U_{\frac{1}{2}}^n.$$

$$q_o^n = q_1^n.$$

## 6. A Right Continuum Boundary

$$P_{j+1}^n = P_j^n \text{ where outside boundary is } j+\frac{1}{2}.$$

## 7. A Left Continuum Boundary

$$P_o^n = P_1^n \text{ where boundary is at } j = \frac{1}{2}.$$

$$q_o^n = q_1^n.$$

$$U_{\frac{1}{2}}^n = U_{\frac{1}{2}}^n \text{ unless } \alpha = 2 \text{ or } 3 \text{ when } U_{\frac{1}{2}}^n = -U_{\frac{1}{2}}^n.$$

## III. THE HOM EQUATION OF STATE SUBROUTINE

HOM is a FORTRAN subroutine which calculates the pressure and temperature given the internal energy, specific volume, and mass function of the solid for solids, gases, and mixtures.

### The Nomenclature

|          |   |
|----------|---|
| $C, S$   | coefficients to a linear fit of $U_s$ and $U_p$               |
| $C1, S1$ | second set of coefficients to a linear fit of $U_s$ and $U_p$ |
| $C_V$    | heat capacity of condensed component (cal/g/deg)              |
| $C'_V$   | heat capacity of gaseous component (cal/g/deg)                |
| $I$      | total internal energy (Mbar-cc/g)                             |
| $P$      | pressure (Mbar)   |
| SPA      | spalling constant to relate spall pressure and tension rate   |
| SPALL P  | interface spalling pressure                                   |
| T        | temperature ( $^{\circ}$ K)                                   |
| USP      | ultimate spalling pressure                                    |
| $U_p$    | particle velocity   |
| $U_s$    | shock velocity  |
| V        | total volume (cc/g)   |
| $V_o$    | initial volume of condensed component (cc/g)                  |

W mass fraction of undecomposed explosive

sive

Subscripts

|     |                     |
|-----|---------------------|
| $g$ | gaseous component   |
| $H$ | Hugoniot            |
| $i$ | isentrope           |
| $s$ | condensed component |

### The Method

#### A. Condensed Components

(The mass fraction, W, is 1; the internal energy, I, is  $I_s$ ; and the specific volume, V, is  $V_g$ ). For volumes less than  $V_o$ , the experimental Hugoniot data are expressed as a linear fit of the shock and particle velocities. The Hugoniot temperatures are computed using the code described in Appendix C.

$$U_s = C + S U_p.$$

$$P_H = \frac{C^2(V_o - V_s)}{[V_o - S(V_o - V_s)]^2}.$$

$$\ln T_H = F_s + G_s \ln V_s + H_s (\ln V_s)^2 + I_s (\ln V_s)^3 + J_s (\ln V_s)^4.$$

$$I_H = \frac{1}{2} P_H (V_o - V_s).$$

$$P_s = \frac{Y_s}{V_s} (I_s - I_H) + P_H, \text{ where } Y_s = V \left( \frac{\partial P}{\partial E} \right)_V. \quad (2)$$

$$T_s = T_H + \frac{(I_s - I_H)(23,890)}{C_V}. \quad (3)$$

Two sets of C and S coefficients may be given. For  $V_s < \text{MINV}$ , the fit  $U_s = C1 + S1(U_p)$  is used with the corresponding changes to the above equations. Between MINV and VSW, the volume is set equal to MINV, and  $U_s = C1 + S1(U_p)$  is used. For volumes greater than  $V_o$ , we use the Grüneisen equation of state and the  $P = 0$  line as the standard curve.

$$P_s = \left[ I_s - \frac{C_V}{(3)(23,890)(\alpha)} \left( \frac{V_s}{V_o} - 1 \right) \right] \frac{V_s}{V_o}.$$

$$T_s = \frac{(I_s)(23,890)}{C_V} + T_o.$$

The spalling option is not used if SPA < 0.0001.

If  $P_s \leq \text{USP}$ , set  $P_s = \text{SPALL P}$  and set spall indicator. If  $P_s \leq \text{SPA} \sqrt{\Delta P / \Delta X}$  ( $\Delta P / \Delta X$  is the tension

rate), and  $P_s \leq SPMIN (5 \times 10^{-3})$ , set  $P_s = SPALL P$  and set spall indicator. Do not spall if neither of the above conditions are satisfied.

### B. Gas Components

(Mass fraction, W, is 0; the internal energy, I, is  $I_g$ ; and the specific volume, V, is  $V_g$ ). The pressure, volume, temperature, and energy values of the detonation products are computed using FORTRAN BKW<sup>8</sup> and fitted by a method of least squares to Eq. (4) through (6). A gamma-law gas may also be fit to these equations as a special case. A code to perform this is described in Appendix C.

$$\ln P_i = A + B \ln V_g + C(\ln V_g)^2 + D(\ln V_g)^3 + E(\ln V_g)^4. \quad (4)$$

$$\ln I_i = K + L \ln P_i + M(\ln P_i)^2 + N(\ln P_i)^3 + O(\ln P_i)^4. \quad (5)$$

$I_i = I_g - Z$  (where Z is a constant used to change the standard state to be consistent with the solid explosive standard state, and if the states are the same is used to keep I positive when making a fit).

$$\ln T_i = Q + R \ln V_g + S(\ln V_g)^2 + T(\ln V_g)^3 + U(\ln V_g)^4. \quad (6)$$

$$-\frac{1}{3} = R + 2S \ln V_g + 3T(\ln V_g)^2 + 4U(\ln V_g)^3.$$

$$P = \left( \frac{1}{3V_i} \right) (I_g - I_i) + P_i. \quad (7)$$

$$T = T_i + \frac{(I_g - I_i)(23,890)}{C'_V} \quad (8)$$

### C. Mixture of Condensed and Gaseous Components

$$(0 < W < 1)$$

$$V = WV_s + (1 - W)V_g.$$

$$I = WI_s + (1 - W)I_g.$$

$$P = P_g = P_s.$$

$$T = T_g = T_s.$$

Multiplying Eq. (3) by  $(W/C_V)$  and Eq. (8) by  $(1 - W)/C_V$  and adding, we get, after substituting T for  $T_s$  and  $T_g$  and I for  $WI_s + (1 + W)I_g$ ,

$$T = \frac{23,890}{C_V W + C'_V(1 - W)} \left\{ I - \left[ WI_H - I_i(1 - W) \right] \right. \\ \left. + \frac{1}{23,890} \left[ T_H C_V W + T_i C'_V(1 - W) \right] \right\}. \quad (9)$$

Equating Eq. (2) and (7) and substituting from (9), we get

$$P_H - P_i + \left( \frac{\gamma_s C_V}{V_s} - \frac{C'_V}{8V_g} \right) \left( \frac{1}{C_V W + C'_V(1 - W)} \left\{ I - \left[ WI_H \right. \right. \right. \\ \left. \left. \left. + I_i(1 - W) \right] + \frac{1}{23,890} \left[ T_H C_V W + T_i C'_V(1 - W) \right] \right\} \right) \\ - \frac{1}{23,890} \left( \frac{\gamma_s C_V T_H}{V_s} - \frac{C'_V T_i}{8V_g} \right) = 0. \quad (10)$$

Knowing V, I, and W, one may use the linear feedback to iterate on either  $V_s$  or  $V_g$  until Eq. (10) is satisfied.

For  $V < V_o$ , we iterate on  $V_s$  with an initial guess of  $V_s = V_o$  and a ratio to get the second guess of 0.999. For  $V \geq V_o$ , we iterate on  $V_g$  with an initial guess of  $V_g = (V - 0.9 V_o W)/(1 - W)$  and a ratio to get the second guess of 1.002.

If the iteration goes out of the physical region ( $V_g \leq 0$  or  $V_s \leq 0$ ), that point is replaced by  $V_s = V_g = V$ . Then knowing  $V_s$  and  $V_g$ , we calculate P and T.

### The Calling Sequence

Call HOM (V, S, G, IND)

V, S, and G are dimensioned arrays of size 5, 23, and 17 numbers, respectively.

V(1) specific volume V

V(2) internal energy I

V(3) mass fraction W

V(4)  $-\left| \frac{\Delta P}{\Delta x} \right|$  input;  
pressure P output

V(5) temperature T output

S(1) C

S(2) S

S(3) VSW

S(4) CL

S(5) SL

S(6) F

S(7) G

S(8) H

S(9) I

|       |            |
|-------|------------|
| S(10) | J          |
| S(11) | $\gamma_s$ |
| S(12) | $C_V$      |
| S(13) | $V_o$      |
| S(14) | $\alpha$   |
| S(15) | SPA        |
| S(16) | USP        |
| S(17) | $T_o$      |
| S(18) | $P_o$      |
| S(22) | SPALL P    |
| S(23) | MINV       |
| G(1)  | A          |
| G(2)  | B          |
| G(3)  | C          |
| G(4)  | D          |
| G(5)  | E          |
| G(6)  | K          |
| G(7)  | L          |
| G(8)  | M          |
| G(9)  | N          |
| G(10) | O          |
| G(11) | Q          |
| G(12) | R          |
| G(13) | S          |
| G(14) | T          |
| G(15) | U          |
| G(16) | $C'_V$     |
| G(17) | Z          |

Ind set to 0 for normal exit, to -1 for iteration error in mixture calculations, and to +1 for a spalled solid.

---

#### APPENDIX A FORTRAN SIN INPUT

The following is a description of the input to FORTRAN SIN.

A few rules for setting up a problem are:

1. The steady-state reaction zone piston is suitable only for slab geometry and only at the left boundary.

2. The gamma-law Taylor wave option assumes that the user is using a gamma-law HOM equation of state. It is suitable only for slab geometry and assumes that the explosive has been burned from right to left. The option assumes that the user is using a right-boundary, initial-final velocity piston and

uses the final velocity as the lowest particle velocity permitted in the detonation products Taylor wave.

3. The real viscosity option is suitable only for slab geometry.

4. The spalling option is suitable only for problems with approximately constant tension gradients and many mesh points.

5. The thermal conductivity option assumes that the system will have uniform thermal conductivity.

6. To restart from tape, one needs only to put the last tape dump number in column 1-5 of the first card. This tape dump number is printed on the listings. When the number in column 1-5 of the first card is greater than 10, the code searches through the tape dumps for a dump at a cycle greater than or equal to the number on the input card. When the proper dump is found, all the variables are read and the calculation proceeds.

#### 1st card

| <u>Col.</u> | <u>Format</u> |   |
|-------------|---------------|---|
| 1-5         | I5            | Number of components or, if > 10, the tape restart cycle number   |
| 6-10        | I5            | Total number of space increments  |
| 11-15       | I5            | Not used  |
| 16-20       | I5            | Not 0 for 4020 output   |
| 21-25       | I5            | Not 0 for graph of pressure vs. radius  |
| 26-30       | I5            | Not 0 for graph of temperature vs. radius   |
| 31-35       | I5            | Not 0 for graph at mass fraction vs. radius   |
| 36-40       | I5            | Not 0 for graph of volume vs. radius  |
| 41-45       | I5            | Not 0 for graph of particle velocity vs. radius   |
| 46-50       | I5            | Not 0 for inclusion of heat conduction  |
| 51-55       | I5            | Left boundary indicator<br>0 for continuum<br>1 for free surface<br>2 for initial velocity-final velocity piston<br>3 for A + BT velocity piston<br>4 for steady-state reaction zone piston |
| 56-60       | I5            | Right boundary indicator  |

|             |               |                                  |             |   |
|-------------|---------------|----------------------------------|-------------|---|
|             |               |                                  |             | <u>Next card</u>                                    |
|             |               | 0 for continuum                  |             |   |
|             |               | 1 for free surface               | <u>Col.</u> | <u>Format</u>                                       |
|             |               | 2 for initial velocity-final ve- | 1-18        | E18.11  |
|             |               | locity piston                    | etc.        | etc.  |
|             |               | 3 for A + BT velocity piston     |             | Right boundary card -                               |
|             |               |                                  |             | same as left boundary card.                         |
|             |               | <u>2nd card</u>                  |             | Again if not a piston, there is                     |
| <u>Col.</u> | <u>Format</u> |                                  |             | no card. A right steady-state                       |
| 1-72        | 12A6          | 72 columns of alphabetic label   |             | reaction zone piston is not per-                    |
|             |               | for problem                      |             | mitted. A right boundary initial-                   |
|             |               |                                  |             | final velocity piston is required                   |
|             |               | <u>3rd card</u>                  |             | if a gamma-law Taylor wave burn                     |
| <u>Col.</u> | <u>Format</u> |                                  |             | is requested.                                       |
| 1-18        | E18.11        | Alpha - 1. for slab geometry     | <u>Col.</u> | <u>Format</u>                                       |
|             |               | 2. for cylindrical geometry      |             |   |
|             |               | 3. for spherical geometry        |             | <u>Next card</u>                                    |
| 19-36       | E18.11        | Print every this many cycles     | 1-18        | E18.11  |
| 37-54       | E18.11        | Graph every this many cycles     |             | If heat conductivity is included,                   |
| 55-72       | E18.11        | Tape dump every this many cycles |             | this card contains:                                 |
|             |               |                                  |             | Heat conduction constant - same                     |
|             |               | <u>4th card</u>                  |             | for all components.                                 |
| <u>Col.</u> | <u>Format</u> |                                  |             | The following cards are present for each component. |
|             |               | Left boundary card - If a left   |             | <u>1st comp. card</u>                               |
|             |               | boundary initial-final piston is | <u>Col.</u> | <u>Format</u>                                       |
|             |               | requested, this card is:         | 1-12        | 2A6   |
| 1-18        | E18.11        | Initial piston velocity          |             | Alphabetic name of component                        |
| 19-36       | E18.11        | Final piston velocity            | <u>Col.</u> | <u>Format</u>                                       |
| 37-41       | I5            | Number of cells from left ini-   | 1-5         | I5  |
|             |               | tially in calculation; if 0, all |             | Number of space increments for                      |
|             |               | cells are used.                  |             | this component                                      |
| 42-46       | I5            | Add on a cell every this many    | 6-10        | I5  |
|             |               | cycles.                          | 11-15       | I5  |
|             |               | If a left-boundary A + BT piston |             | Not 0 for gas or explosive                          |
|             |               | is requested, this card is:      | 16-20       | I5  |
| 1-18        | E18.11        | A                                |             | 0 for Arrhenius burn, 1 for C-J                     |
| 19-36       | E18.11        | B                                |             | volume burn, 2 for gamma-law Tay-                   |
| 37-41       | I5            | Same as initial-final piston     |             | lor wave  |
| 42-46       | I5            | Same as initial-final piston     | <u>Col.</u> | <u>Format</u>                                       |
|             |               | If a left steady-state piston is | 1-18        | E18.11  |
|             |               | requested, this card is:         | 19-36       | E18.11  |
| 1-18        | E18.11        | Detonation velocity              | 37-54       | E18.11  |
| 19-36       | E18.11        | Spike volume                     | 55-72       | E18.11  |
| 37-41       | I5            | Same as initial-final piston     |             | Space increment (cm)                                |
| 42-46       | I5            | Same as initial-final piston     |             | Time increment ( $\mu$ sec)                         |
|             |               | If a piston is not requested, no |             | Viscosity factor                                    |
|             |               | card appears for the left bound- |             | Initial density (g/cc)                              |
|             |               | ary.                             |             | <u>3rd comp. card</u>                               |
|             |               |                                  |             |   |
|             |               |                                  |             | <u>4th comp. card</u>                               |
|             |               |                                  | <u>Col.</u> | <u>Format</u>                                       |
|             |               |                                  | 1-18        | E18.11  |
|             |               |                                  | 19-36       | E18.11  |
|             |               |                                  | 37-54       | E18.11  |
|             |               |                                  | 55-72       | E18.11  |
|             |               |                                  |             | Initial pressure (Mbar)                             |
|             |               |                                  |             | Initial temperature ( $^{\circ}$ K)                 |
|             |               |                                  |             | Initial internal energy (Mbar-                      |
|             |               |                                  |             | cc/g)   |
|             |               |                                  |             | Initial velocity (cm/ $\mu$ sec)                    |

#### 5th-10th comp. card

Six cards of solid parameters for equation of state and elastic-plastic calculations. The variables are four per card with each card of the format 4E18.11. They are, in order: C, S, VSW, Cl, Sl, F, G, H, I, J, Y<sub>s</sub>, C<sub>V</sub>, V<sub>o</sub>, α, SPA, USP, T<sub>o</sub>, P<sub>o</sub>, 2/3 Y<sub>o</sub>, μ, PLAP, SPALL P, and MINV.

#### 11th comp. card

| Col.  | Format |  |
|-------|--------|--|
| 1-18  | E18.11 | Initial mass fraction of the solid   |
| 19-36 | E18.11 | Frequency factor for Arrhenius burn  |
| 37-54 | E18.11 | Activation energy for Arrhenius burn                                       |
| 55-72 | E18.11 | Volume for C-J burn or C-J detonation velocity for a gamma-law Taylor wave |

For a pure solid there are no more cards.

For a gas or explosive we have,

#### 12th-16th comp. cards

Five cards of gas equation of state parameters. The variables are four to a card with each card of the format 4E18.11. They are, in order: A, B, C, D, E, K, L, M, N, O, Q, R, S, T, U, C'<sub>V</sub>, and Z.

### APPENDIX B THE FORTRAN SIN CODE

In this appendix we list the names or symbols of the variables in SIN both as used in the FORTRAN code and in this report. The listing of the FORTRAN code as it existed at the time of preparation of this report is also presented. Errors in this version of the code will be corrected as they become known to the authors. Anyone wishing to actually copy any part of this code should contact the authors for the latest version.

#### Variables Used in FORTRAN SIN

| Code Name                    | Report Symbol                     |
|------------------------------|-----------------------------------|
| CR - cell radius             | R <sub>j-1/2</sub> <sup>n+1</sup> |
| CRO - previous cell radius   | R <sub>j-1/2</sub> <sup>n</sup>   |
| CU - cell velocity           | U <sub>j-1/2</sub> <sup>n+1</sup> |
| CUO - previous cell velocity | U <sub>j-1/2</sub> <sup>n</sup>   |

|   |                               |
|---|-------------------------------|
| CV - cell volume  | V <sub>j</sub> <sup>n+1</sup> |
| CVO - previous cell volume  | V <sub>j</sub> <sup>n</sup>   |
| CM - cell mass  | M <sub>j</sub>                |
| CQ - cell viscosity   | Q <sub>j</sub> <sup>n</sup>   |
| ICF - cell flag word  |                               |
| XXYY <sub>i</sub> - YY component index  |                               |
| - XX spall flag   |                               |
| 0 - no spall  |                               |
| 1 - spalled cell  |                               |
| 2 - interface cell  |                               |
| CW - cell mass fraction   | W <sub>j</sub> <sup>n+1</sup> |
| CWO - previous cell mass fraction   | W <sub>j</sub> <sup>n</sup>   |
| CT - cell temperature   | T <sub>j</sub> <sup>n</sup>   |
| CP - cell pressure  | P <sub>j</sub> <sup>n</sup>   |
| CS - cell stress deviator in x or r direction   | S <sub>xj</sub> <sup>n</sup>  |
| CSZ - cell stress deviator in z direction   | S <sub>zj</sub> <sup>n</sup>  |
| CI - cell internal energy   | I <sub>j</sub> <sup>n+1</sup> |
| CIO - previous cell internal energy   | I <sub>j</sub> <sup>n</sup>   |
| LABEL - 12 words containing 72 columns of alphabetic information - the problem label - format 12A6                                  |                               |
| TTIME - total time elapsed in problem   |                               |
| DELT - time increment for this cycle  |                               |
| ICYCL - cycle number  |                               |
| PCNT - count for printing   |                               |
| GCNT - count for graphing   |                               |
| DCNT - count for dumping  |                               |
| PINC - print every PINC cycles  |                               |
| GINC - graph every GINC cycles  |                               |
| DINC - dump every DINC cycles   |                               |
| IALPH - 0 for slab, 1 for cylinder, 2 for sphere  |                               |
| HEATC - heat conductivity constant  |                               |
| GASW - set W to 0 if less than GASW   |                               |
| NCL - total number of cells in calculation  |                               |
| PTMIN - the pressure of one cell of a component must be greater than PTMIN ( $1. \times 10^{-5}$ ) to use that component's delta t. |                               |
| IPNT - unused   |                               |

IMC - not 0 for microfilm output  
 IPR - not 0 for a pressure vs. radius graph  
 ITR - not 0 for a temperature vs. radius graph  
 IWR - not 0 for a mass fraction vs. radius graph  
 IIR - not 0 for an internal energy vs. radius graph  
 IUR - not 0 for a particle velocity vs. radius graph  
 IHG - not 0 to include heat conduction  
 ILB - left boundary indicator

| <u>At Read-In</u>   | <u>During Execution</u> |                                   |
|---|-------------------------|-----------------------------------|
| 0   | 1                       | free surface                      |
| 1   | 2                       | continuum                         |
| 2   | 3                       | initial-final piston              |
| 3   | 4                       | A + BT piston                     |
| 4   | 5                       | steady-state reaction zone piston |
| IRB - right boundary indicator (same as left except no reaction zone piston)  |                         |                                   |
| WSW - W to switch from initial to final for that piston   |                         |                                   |
| WMAX - for $W > WMAX (0.99)$ in C-J burn, $P = P_0$   |                         |                                   |
| SMIN - change in stress set to 0 if less than $SMIN (1.0 \times 10^{-9})$   |                         |                                   |
| ALB, BLB - left boundary piston constants:<br>either initial and final velocities<br>or A and B in A + BT   |                         |                                   |
| ARB, HRB - right boundary piston constants (same as left)   |                         |                                   |
| NLI - number of cells initially in calculation from left. If 0, all cells are used.   |                         |                                   |
| NLINC - add on a cell from left every NLINC cycles  |                         |                                   |
| NLCNT - count for adding on cells from left   |                         |                                   |
| NRI, NRINC, NRCNT - same as above, only from right. Note: These numbers are used only if there is a piston at their respective boundaries. If there is no piston specified, all cells are used. |                         |                                   |
| NLH - number of cells from the left in calculation at the time of interest  |                         |                                   |
| NRL - index of lowest cell in calculation from right end  |                         |                                   |

DX - at input-space increment for each component during calculation - space increment at right-most component  
 E - activation energy for Arrhenius burn  
 GAS - gas parameters  
 SOL - solid parameters  
 VCJ - C-J burn volume  
 VFACT - viscosity factor  
 Z - frequency factor for Arrhenius burn  
 NAM - alphabetic names of components (2 words per component)  
 DTIME - delta t for each component  
 NINC - number of space increments for each component  
 NCOM - number of components  
 IEXP - not 0 for explosive or gas  
 IERN - 0 for Arrhenius burn, 1 for C-J volume burn, 2 for gamma-law Taylor wave  
 IVIS - 0 for PIC viscosity, 1 for Landshoff form, 2 for real form  
 ALPH - 1 for slab, 2 for cylinder, 3 for sphere  
 RHOO - initial density, only for the component being read  
 P0 - initial pressure, only for the component being read  
 T0 - initial temperature, only for the component being read  
 EO - initial internal energy, only for the component being read  
 U0 - initial particle velocity, only for the component being read  
 W0 - initial mass fraction, only for the component being read  
 NINC - number of space increments for this component  
 RFRNT - r coordinate value of the nearest spalled or interface cell of the same component with a lower index  
 EQ - five parameters used to call HOM. EQ(1) - volume, EQ(2) - energy, EQ(3) - mass fraction, EQ(4) -  $|\Delta P/\Delta X|$  for spall input or pressure output, EQ(5) - temperature output  
 INDH - HOM indicator -1 error, 0 normal, +1 spalled  
 X - elastic-plastic ratio of P/PLAP, not greater than 1  
 DELS - change in stress deviator  
 TKE - total kinetic energy of each component

TIE - total internal energy of each component  
LIN - line counter for printing  
KIND - the index of cell on right-hand boundary  
DCJ - C-J detonation velocity for gamma-law Taylor  
wave burn  
DRT - total delta R for gamma-law Taylor wave burn  
DRF - first R for gamma-law Taylor wave burn  
DRL - last R for gamma-law Taylor wave burn  
UCJ, PCJ, VCR, CCJ - C-J values for gamma-law  
Taylor wave burn  
COK -  $(\gamma - 1)/(\gamma + 1)$  for gamma-law Taylor wave  
burn  
COL - UCJ -  $\frac{2C}{\gamma - 1}$  for gamma-law Taylor wave burn  
RXZDV - steady-state reaction zone piston detona-  
tion velocity  
RXZVS - steady-state reaction zone piston spike  
volume guess

Listing of the FORTRAN Code

```

PROGRAM FSIN (INPUT,OUTPUT,FILM,TAPE12=FILM,TAPE1)
C      CELL RADIUS J-1/2
C      CELL VELOCITY J-1/2
C      CELL VOLUME J
C      CELL MASS J
C      CELL VISCOSITY J
C      CELL FLAG WORD J
C      CELL MASS FRACTION J
C      CELL TEMPERATURE J
C      CELL PRESSURE J
C      CELL STRESS DEVIATOR J
C      CELL STRESS DEVIATOR IN Z DIRECTION J
C      CELL INTERNAL ENERGY J
000003  COMMON CR(999),CRO(999),CU(999),CUO(999),CV(999),CVO(999),
        1CM(999),CQ(999),ICF(999),CW(999),CWO(999),CT(999),CP(999),
        2CS(999),CSZ(999),CI(999),CIO(999),LABEL(12)
000003  COMMON /MISC/ TTIME,DELT,ICYCL,PCNT,GCNT,DCNT,DINC,PINC,GINC,
        1IALPH,HEATC,GASW,NCL,PTMIN,IPNT,IMC,IPR,ITR,IWR,IIR,IUR,IHC,ILB,
        2IRB,WSW,PSMIN,WMAX,SMIN,ALB,BLB,ARB,BRB,NLI,NRI,NLINC,NRINC,
        3NLCNT,NRCNT,NLH,NRL,DX,KIND,RXZDV,RXZVS,FPO,FE0,RXZ
000003  COMMON /MATER/ E(10),GAS(17,10),IBRN(10),SOL(23,10),VCJ(10),
        1VFACT(10),Z(10),NAM(2,10),DTIME(10),NOINC(10),IVIS(10),IEXP(10),
        2NCOM
000003  DIMENSION RXZ(10),EQ(5)
000003  C      WSW   W TO SWITCH PISTON VELOCITY FROM INITIAL TO FINAL
000003  DATA WSW /0.02/
000003  DATA NRI /0/
000003  DATA NLI /0/
000003  DATA NLH /1/
000003  C      COUNTS ARE SET LARGE SO CELLS AREN'T ADDED ON IF NOT REQUESTED
000003  DATA NRCNT/100000/
000003  DATA NLCNT/100000/
000003  C      READ INPUT DATA
000003  C      NCOM   NUMBER OF COMPONENTS OR RESTART CYCLE NUMBER
000003  C      NCL    TOTAL NUMBER OF CELLS IN THE CALCULATION
000003  C      IPNT   UNUSED
000003  C      IMC    NOT 0 FOR MICROFILM OUTPUT
000003  C      IPR    NOT 0 TO GIVE A GRAPH OF PRESSURE
000003  C      ITR    NOT 0 TO GIVE A GRAPH OF TEMPERATURE
000003  C      IWR    NOT 0 TO GIVE A GRAPH OF MASS FRACTION
000003  C      IIR    NOT 0 TO GIVE A GRAPH OF VOLUME
000003  C      IUR    NOT 0 TO GIVE A GRAPH OF PARTICLE VELOCITY
000003  C      IHC    NOT 0 FOR CALCULATION OF HEAT CONDUCTION IN ENERGY
000003  C      ILB    LEFT HAND BOUNDARY INDICATOR
000003  C          = 0 FOR CONTINUUM
000003  C          = 1 FOR FREE SURFACE
000003  C          = 2 FOR INITIAL-FINAL PISTON
000003  C          = 3 FOR A+BT PISTON
000003  C          = 4 FOR STEADY STATE REACTION ZONE SLAB PISTON
000003  C      IRB    RIGHT HAND BOUNDARY INDICATOR
000003  C          = 0 FOR CONTINUUM
000003  C          = 1 FOR FREE SURFACE
000003  C          = 2 FOR INITIAL-FINAL PISTON
000003  C          = 3 FOR A+BT PISTON
000003  C      READ 901,NCOM,NCL,IPNT,IMC,IPR,ITR,IWR,IIR,IUR,IHC,ILB,IRB
000003  C      SEE IF TAPE RESTART
000037  C      IF (NCOM.GT.10) GO TO 500
000043  C      LABEL 72 COLUMNS OF ALPHABETIC COMMENT
000043  C      READ 900,LABEL
000043  C          ALPH = 1. FOR SLAB
000043  C          = 2. FOR CYLINDER

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C      * 3. FOR SPHERE
C      PINC   PRINT EVERY PINC CYCLES
C      GINC   GRAPH EVERY GINC CYCLES
C      DINC   DUMP EVERY DINC CYCLES
000050  READ 902,ALPH,PINC,GINC,DINC
000064  IALPH=ALPH-1.
C      READ IN PISTON QUANTITIES
C      ALB,BLB  PISTON CONSTANTS FOR LEFT PISTON
C      NLI      NUMBER OF CELLS INITIALLY IN CALCULATION FROM LEFT
C      NLINC   ADD ON A CELL FROM LEFT EVERY NLINC CYCLES
C      RXZDV   STEADY STATE REACTION ZONE PISTON DETONATION VELOCITY
C      RXZVS   STEADY STATE REACTION ZONE PISTON GUessed SPIKE VOLUME
000067  IF (ILB.EQ.2.OR.ILB.EQ.3) READ 903,ALB,BLB,NLI,NLINC
000111  IF(ILB.EQ.4) READ 903,RXZDV,RXZVS,NLI,NLINC
C      NRI      NUMBER OF CELLS INITIALLY IN CALCULATION FROM RIGHT
C      NRINC   ADD ON A CELL FROM RIGHT EVERY NRINC CYCLES
C      ARR,BRB  PISTON CONSTANTS FOR RIGHT PISTON
000127  IF (IRB.EQ.2.OR.IRB.EQ.3) READ 903,ARB,BRB,NRI,NRINC
C      READ IN HEAT CONSTANT
000152  IF (IHC.NE.0) READ 902,HEATC
000161  K=2
000162  CR(2)=0.
000163  CR(2)=0.
C      IALPH = 0 FOR SLAB
C          1 FOR CYLINDER
C          2 FOR SPHERE
000164  IF (IALPH.EQ.0) PRINT 904,LABEL
000172  IF (IALPH.EQ.1) PRINT 905,LABEL
000202  IF (IALPH.EQ.2) PRINT 906,LABEL
000212  PRINT 907,NCOM
000220  PRINT 908,NCL
000226  IF (ILB.EQ.0) PRINT 909
000233  IF (ILB.EQ.1) PRINT 910
000241  IF (ILB.EQ.2) PRINT 911,ALB,BLB,WSW,NLI,NLINC
000261  IF (ILB.EQ.3) PRINT 912,ALB,BLB,NLI,NLINC
000277  IF (ILB.EQ.4) PRINT 930,RXZDV,RXZVS,NLI,NLINC
000315  IF (IRB.EQ.0) PRINT 913
000322  IF (IRB.EQ.1) PRINT 914
000330  IF (IRB.EQ.2) PRINT 915,ARB,BRB,WSW,NRI,NRINC
000350  IF (IRB.EQ.3) PRINT 916,ARB,BRB,NRI,NRINC
000366  PRINT 917
C      DO 4020 PRINTING IF REQUESTED
000372  IF (IMC.EQ.0) GO TO 1
C      *****4020 OUTPUT BELOW*****
C      4020 OUTPUT BELOW
C      ****4020 OUTPUT BELOW*****
000373  IF (IALPH.EQ.0) WRITE (12,904) LABEL
000402  IF (IALPH.EQ.1) WRITE (12,905) LABEL
000412  IF (IALPH.EQ.2) WRITE (12,906) LABEL
000422  WRITE (12,907) NCOM
000430  WRITE (12,908) NCL
000436  IF (ILB.EQ.0) WRITE (12,909)
000443  IF (ILB.EQ.1) WRITE (12,910)
000451  IF (ILB.EQ.2) WRITE (12,911) ALB,BLB,WSW,NLI,NLINC
000471  IF (ILB.EQ.3) WRITE (12,912) ALB,BLB,NLI,NLINC
000507  IF (ILB.EQ.4) WRITE (12,930) RXZDV,RXZVS,NLI,NLINC
000525  IF (IRB.EQ.0) WRITE (12,913)
000532  IF (IRB.EQ.1) WRITE (12,914)
000540  IF (IRB.EQ.2) WRITE (12,915) ARB,BRB,WSW,NRI,NRINC
000560  IF (IRB.EQ.3) WRITE (12,916) ARB,BRB,NRI,NRINC
000576  WRITE (12,917)
C      ****4020 OUTPUT BELOW*****

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C          4020 OUTPUT ABOVE
C #####
C READ DATA AND SET UP MESH FOR EACH COMPONENT
000602 1 DO 10 I=1,NCOM
C      NAM      NAME OF COMPONENT
000604      READ 900,NAM(1,I),NAM(2,I)
C      NINC     NUMBER OF SPACE INCREMENTS FOR THIS COMPONENT
C      IEXP     NOT 0 FOR GAS OR EXPLOSIVE
C      IBRN     = 0 FOR ARREHENIUS BURN
C              = 1 FOR CJ VOLUME BURN
C              = 2 FOR GAMMA LAW TAYLOR WAVE
C      IVIS    = 0 FOR PIC VISCOSITY
C              = 1 FOR LANDSHOFF VISCOSITY
C              = 2 FOR REAL VISCOSITY
000617      READ 901,NINC,IEXP(I),IBRN(I),IVIS(I)
C      DX       SPACE INCREMENT IN CENTIMETERS
C      DTIME   TIME INCREMENT IN MICROSECONDS
C      VFACT   VISCOSITY FACTOR
C      RH00   INITIAL DENSITY
000633      READ 902,DX,DTIME(I),VFACT(I),RH00
C      P0       INITIAL PRESSURE
C      T0       INITIAL TEMPERATURE
C      E0       INITIAL INTERNAL ENERGY
C      U0       INITIAL VELOCITY
C      SOL(J,I) SOLID EQUATION OF STATE AND ELASTIC-PLASTIC CONSTANTS
000647      READ 902,P0,T0,E0,U0
000663      IF(I.GT.1) GO TO 11
000667      FPO = P0
000670      FEO = E0
000671 11 READ 902,(SOL(J,I),J=1,23)
C      W0       INITIAL MASS FRACTION
C      Z        FREQUENCY FACTOR FOR ARREHENIUS BURN
C      E        ACTIVATION ENERGY FOR ARREHENIUS BURN
C      VCJ     VOLUME FOR CJ BURN OR DET VEL FOR GAMMA LAW TAYLOR WAVE
000705      READ 902,W0,Z(I),E(I),VCJ(I)
000721      PRINT 918,NAM(1,I),NAM(2,I),NINC,DX,DTIME(I)
000743      IF (IEXP(I).EQ.0) GO TO 2
000745      READ 902,(GAS(J,I),J=1,17)
000760      PRINT 919
000764      IF (IBRN(I).EQ.0) PRINT 921,E(I),Z(I)
000775      IF (IBRN(I).EQ.1) PRINT 922,VCJ(I),GASW
001007      IF (IBRN(I).EQ.2) PRINT 929,VCJ(I)
001017 2 IF (IVIS(I).FQ.0) PRINT 923,VFACT(I)
001026      IF (IVIS(I).EQ.1) PRINT 924,VFACT(I)
001036      IF (IVIS(I).FQ.2) PRINT 925,VFACT(I)
001046      PRINT 926,RH00,P0,T0,E0,U0,W0
001066      PRINT 927,(SOL(J,I),J=1,23)
001102      IF (IEXP(I).NE.0) PRINT 928,(GAS(J,I),J=1,17)
001117      IF (IMC.EQ.0) GO TO 4
#####
C          4020 OUTPUT BELOW
C #####
001120      WRITE (12,918) NAM(1,I),NAM(2,I),NINC,DX,DTIME(I)
001142      IF (IEXP(I).EQ.0) GO TO 3
001144      WRITE (12,919)
001147      IF (IBRN(I).EQ.0) WRITE (12,921) E(I),Z(I)
001160      IF (IBRN(I).EQ.1) WRITE (12,922) VCJ(I),GASW
001172      IF (IBRN(I).EQ.2) WRITE (12,929) VCJ(I)
001202 3 IF (IVIS(I).EQ.0) WRITE (12,923) VFACT(I)
001211      IF (IVIS(I).EQ.1) WRITE (12,924) VFACT(I)
001221      IF (IVIS(I).FQ.2) WRITE (12,925) VFACT(I)
001231      WRITE (12,926) RH00,P0,T0,E0,U0,W0

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001251      WRITE (12,927) (SOL(J,I),J=1,23)
001265      IF (IEXP(I).NE.0) WRITE (12,928) (GAS(J,I),J=1,17)
001265      C
001265      **** 4020 OUTPUT ABOVE ****
001265      C
001265      FILL IN CELL VALUES FOR THIS COMPONENT
001302      DO 9 J=1,NINC
001304      4 IF(IBRN(I).EQ.2) GO TO 12
001307      CRO(K+1)=CRO(K)+DX
001312      CR(K+1)=CRO(K+1)
001313      CUO(K)=U0
001315      CU(K)=CUO(K)
001316      CP(K)=P0
001320      CT(K)=T0
001321      CW0(K)=W0
001323      CW(K)=CW0(K)
001324      CSZ(K) = 0.
001325      CS(K) = 0.
001326      CIO(K)=E0
001330      CI(K)=CIO(K)
001331      CM(K)=RH00*DX*((CRO(K)+CRO(K+1))*,.5)**IALPH
001342      CVO(K)=1./RH00
001344      CV(K)=CVO(K)
001345      ICF(K)=I
001347      CQ(K)=0.
001350      K=K+1
001351      9 CONTINUE
001354      C SET SPALL FLAG FOR INTERFACE BETWEEN COMPONENTS
001356      17 IF (IEXP(I).NE.0) GO TO 18
001356      ICF(K-NINC)=ICF(K-NINC)+128
001361      18 NOINC(I) = NTNC
001363      10 CONTINUE
001366      C SET RIGHT AND LEFT BOUNDARY VALUES
001367      CM(1)=CM(2)
001367      CM(K)=RH00*DX*(CRO(K)+DX*.5)**IALPH
001400      CQ(K)=0.
001401      KIND=K
001402      CRO(1)=-CRO(3)
001404      CRO(K+2)=CRO(K+1)+DX
001406      CI(1)=0.
001406      CS(1)=0.
001407      CSZ(1)=0.
001410      CV(1)=0.
001411      CV(K)=0.
001412      CS(K)=0.
001413      CSZ(K)=0.
001414      CI(K)=0.
001415      ILB=ILB+1
001416      IRB=IRB+1
001417      TTIME=0.
001420      DELT=0.
001421      C FIND MAXIMUM DELTA T FOR FIRST CYCLE
001421      DO 20 I=1,NCOM
001422      IF (DELT.LT.DTIME(I)) DELT=DTIME(I)
001426      20 CONTINUE
001431      C SET UP NUMBER OF CELLS IN CALCULATION
001431      NRL=NCL+2
001433      C SEE IF THERE IS A LEFT PISTON
001433      IF(ILB.LT.2) GO TO 24
001433      C GO TO 22 IF CELL ADDING ON NOT REQUESTED
001434      IF (NLI.EQ.0) GO TO 22
001434      C SET NUMBER OF CELLS FROM LEFT AND COUNT FOR ADDING ON CELLS

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001435      NLH=NLI+1
001437      NLCNT=NLINC
001440      C SEE IF THERE IS A RIGHT PISTON
001441      IF(IRB.LT.2) GO TO 90
001442      C ARE CELLS TO BE ADDED ON FROM RIGHT
001443      IF (NRI.EQ.0) GO TO 90
001444      C SET INITIAL NUMBER OF CELLS FROM RIGHT AND COUNT FOR ADDING ON
001445      21 NRL=NCL+1-NRI
001446      NRCNT=NRINC
001447      C CHECK TO SEE IF ALL CELLS IN CALCULATION
001448      IF (NRL.GT.NLH+1) GO TO 90
001449      C USE ALL CELLS IN CALCULATION
001450      22 NLH=NCL+1
001451      NLI=1
001452      NRI=0
001453      GO TO 90
001454      C SEE IF THERE IS A RIGHT PISTON
001455      24 IF(IRB.LT.2) GO TO 22
001456      C ARE CELLS TO BE ADDED ON FROM RIGHT
001457      IF (NRI.EQ.0) GO TO 22
001458      NLH = 1
001459      GO TO 21
001460      C SET LEFT BOUNDARY VALUES
001461      90 GO TO (100,110,120,130,140),ILB
001462      C LEFT BOUNDARY CONTINUUM
001463      100 CP(1)=CP(2)
001464      CR(1)=CR(2)-CR(3)
001465      CQ(1)=CQ(2)
001466      CU(1)=-CU(2)
001467      IF (IALPH.EQ.0) CU(1)=CU(2)
001468      CU0(1)=CU(1)
001469      CT(1)=CT(2)
001470      GO TO 190
001471      C LEFT BOUNDARY FREE SURFACE
001472      110 CP(1)=-CP(2)
001473      CR(1)=CR(2)-CR(3)
001474      CQ(1)=CQ(2)
001475      CU(1)=-CU(2)
001476      CU0(1)=CU(1)
001477      CT(1)=CT(2)
001478      GO TO 190
001479      C LEFT BOUNDARY PISTON - INITIAL.FINAL
001480      120 CQ(1)=CQ(2)
001481      CR(1)=CR(2)-CR(3)
001482      CP(1)=CP(2)
001483      CT(1)=CT(2)
001484      IF (CW(4).LT.WSW) GO TO 125
001485      CU(1)=ALB
001486      CU0(1)=CU(1)
001487      CU(2)=CU(1)
001488      CU0(2)=CU0(1)
001489      GO TO 190
001490      125 CU(1)=BLB
001491      CU0(1)=CU(1)
001492      CU(2)=CU(1)
001493      CU0(2)=CU0(1)
001494      GO TO 190
001495      C LEFT BOUNDARY PISTON - A+BT
001496      130 CQ(1)=CQ(2)
001497      CR(1)=CR(2)-CR(3)
001498      CP(1)=CP(2)
001499      CT(1)=CT(I)

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001560      CU(I)=ALB+BLB*TTIME
001563      CU0(1)=CU(1)
001564      CU(2)=CU(1)
001565      CU0(2)=CU0(1)
001567      C   SET RIGHT BOUNDARY VALUES
001568      190 GO TO (200,210,220,230),IR8
001569      C   RIGHT BOUNDARY CONTINUUM
001570      200 CT(K)=CT(K-1)
001571      CP(K)=CP(K-1)
001572      CU(K)=CU(K-1)
001573      CU0(K)=CU(K)
001574      GO TO 290
001575      C   RIGHT BOUNDARY FREE SURFACE
001576      210 CT(K)=CT(K-1)
001577      CP(K)=-CP(K-1)
001578      CU(K)=CU(K-1)
001579      CU0(K)=CU(K)
001580      GO TO 290
001581      C   RIGHT BOUNDARY PISTON - INITIAL,FINAL
001582      220 CT(K)=CT(K-1)
001583      CP(K)=CP(K-1)
001584      IF (CW(K-3).LT.WSW) GO TO 225
001585      CU(K)=ARB
001586      CU0(K)=ARB
001587      GO TO 290
001588      225 CU(K)=BRB
001589      CU0(K)=BRB
001590      GO TO 290
001591      C   RIGHT BOUNDARY PISTON - A+BT
001592      230 CT(K)=CT(K-1)
001593      CP(K)=CP(K-1)
001594      CU(K)=ARB+BRB*TTIME
001595      CU0(K)=CU(K)
001596      290 CONTINUE
001597      IF (NLI.NE.0) CALL VELOC (2,NLH)
001598      IF (NRI.NE.0) CALL VELOC (NRL,NCL+1)
001599      IF (NLI.NE.0) CALL RADIUS (2,NLH+1)
001600      IF (NRI.NE.0) CALL RADIUS (NRL,NCL+2)
001601      C   SET RADIUS FOR CELL BEYOND RIGHT BOUNDARY
001602      CR(K+2)=CR(K+1)+DX
001603      IF (NLI.NE.0) CALL VOLUM (2,NLH)
001604      IF (NRI.NE.0) CALL VOLUM (NRL,NCL+1)
001605      IF (NLI.NE.0) CALL ENERGY (2,NLH)
001606      IF (NRI.NE.0) CALL FNERGY (NRL,NCL+1)
001607      IF (IHC.EQ.0) GO TO 300
001608      IF (NLI.NE.0) CALL HETCON (2,NLH)
001609      IF (NRI.NE.0) CALL HFTCON (NRL,NCL+1)
001610      300 IF (NLI.NE.0) CALL VISCOS (2,NLH)
001611      IF (NRI.NE.0) CALL VISCOS (NRL,NCL+1)
001612      IF (NLI.NE.0) CALL BURN (2,NLH)
001613      IF (NRI.NE.0) CALL BURN (NRL,NCL+1)
001614      C   SET W NEAR AXIS
001615      CW(2)=CW(4)
001616      CW(3)=CW(4)
001617      IF (NLI.NE.0) CALL STRESS (2,NLH)
001618      IF (NRI.NE.0) CALL STRESS (NRL,NCL+1)
001619      IF (NLI.NE.0) CALL EQST (2,NLH)
001620      IF (NRI.NE.0) CALL EQST (NRL,NCL+1)
001621      IF (NLI.NE.0) CALL UPDATE (1,NLH+2)
001622      IF (NRI.NE.0) CALL UPDATE (NRL,NCL+3)
001623      CALL TIME
001624      GO TO 90

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C      RESTART FROM TAPE
002000 500 IRST=NCOM
C      SEARCH FOR DUMP WITH PROPER CYCLE NUMBER
002002 501 READ (1) CRO,CUO,CWO,CSZ,CIO,CVO,ICF,CM,CQ,CT,CP,LABEL,DELT,HEATC,
        IIALPH,TTIME,PINC,GINC,DINC,PCNT,GCNT,DCNT,E,GAS,IBRN,SOL,VCJ,
        2VFACT,Z,NAM,DTIME,NOINC,NCOM,ICYCL,NCL,IPNT,IMC,IPR,ITR,IWR,IIR,
        3IUR,IHC,ILB,IRB,ALB,BLB,ARB,BRB,WSW,NLI,NRI,NLINC,NRINC,NLCNT,
        4NRCNT,NLH,NRL,DX,IVIS,IEAP,KIND,CR,CI,CW,CV,CU,CS,RXZDV,RXZVS,
        SRXZ,FPO,FEQ
002227 K=KIND
002231 IF (IRST.GT.ICYCL) GO TO 501
002234 GO TO 90
C      THE SLAB GAMMA LAW TAYLOR WAVE ## ASSUMES DETONATION WAVE MOVED
C      FROM RIGHT TO LEFT AND HAS BRB FINAL PARTICLE VELOCITY
002234 12 L = K
002236 DO 13 J=1,NINC
002237 CR(L+1) = CR(L) + DX
002242 CT(L)=T0
002244 CWO(L)=0.
002245 CW(L)=0.
002246 CSZ(L)=0.
002247 CS(L)=0.
002250 CM(L)=RHOO*DX
002252 CQ(L)=0.
002253 ICF(L)=I
002254 L=L+1
002256 13 CONTINUE
002260 DCJ=VCJ(I)
002261 DRT=CR(L)-CR(K)
002264 DRF=CR(K)
002266 DRL=CR(L)
002267 UCJ=DCJ/(-GAS(2,I)+1.)
002274 PCJ=(RHOO)*(DCJ*DCJ)/(-GAS(2,I)+1.)
002300 VCJR=L-GAS(2,I))/((-GAS(2,I)+1.)*RHOO)
002305 CCJ=DCJ-UCJ
002307 COK=(-GAS(2,I)-1.)/(-GAS(2,I)+1.)
002313 COL=UCJ-((2./(-GAS(2,I)-1.))*CCJ)
002320 COT=DRT/DCJ
002322 DO 14 J=1,NINC
002324 COY=(DRL-CR(K))/COT
002330 CU(K)=(2.*COY)/(-GAS(2,I)+1.)+COK*COL
002341 CP(K)=PCJ*(((-GAS(2,I)-1.)*0.5)*(CU(K)-COL))/CCJ+*(-GAS(2,I)*2./
1*(-GAS(2,I)-1.))
002361 CV(K)=(PCJ*(VCJR*(-GAS(2,I)))/CP(K))** (1./(-GAS(2,I)))
002376 CVO(K)=CV(K)
002400 CI(K)=(CP(K)*CV(K))/(-GAS(2,I)-1.)-(PCJ*VCJR)/(-GAS(2,I)-1.)
1+ 0.5*PCJ*(1./RHOO-VCJR)
002417 CIO(K)=CI(K)
002421 DRP=CM(K)*CV(K)
002423 CR(K+1)=CR(K)+DRP
002425 CRO(K+1)=CR(K+1)
002426 CU(K)=-CU(K)
002430 CUO(K)=CU(K)
002431 IF (CU(K).GT.BRB) GO TO 15
002435 K=K+1
002436 14 CONTINUE
002440 GO TO 17
002441 15 L=K
002443 DO 16 N=J,NINC
002445 CU(K)=CU(L)
002450 CUO(K)=CU(L)
002451 CP(K)=CP(L)

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002453      CV(K)=CV(L)
002454      CVO(K)=CV(L)
002456      CI(K)=CI(L)
002457      CIO(K)=CI(L)
002461      CR(K+1)=CR(K)+DRP
002463      CRO(K+1)=CR(K+1)
002465      K=K+1
002466      16 CONTINUE
002470      GO TO 17
C      REACTION ZONE PISTON
C      FOR SLABS AT LEFT BOUNDARY ONLY
002471      DATA RXZ(1)/ 0./
002471      DATA RXZ(2) /1.001/
002471      DATA RXZ(3) //1.0E-5/
002471      DATA RXZ(10)/ 0./
002471      140 IF(RXZ.EQ.0.) RXZ=RXZVS
002473      IF(CW(4).LT.GASW) GO TO 120
002475      CALL LFB (RZV,RZF,RXZ)
002500      IF(RXZ(10)) 141,142,143
002502      141 PRINT 931,RXZ
002510      PCNT=1.
002512      GCNT=100.
002513      ICYCL=ICYCL-1
002515      TTIME=TTIME-DELT
002517      CALL TIME
002520      STOP
002522      931 FORMAT (33H1 REACTION ZONE PISTON LFB ERROR , 5E18.11)
002522      143 RZI=FEO + 0.5/( SOL(13,I)*SOL(13,I)*RXZDV*RXZDV*(SOL(13,I)-
1RZV)**2)
002535      EQ(1)=RZV
002536      EQ(2)=RZI
002537      160 EQ(3)=CW(4)
002541      CALL HOM (EQ,SOL(1,I),GAS(1,I),INDH)
002550      IF(INDH) 144,145,144
002551      144 PRINT 932,I,EQ
002561      932 FORMAT (33H1 HOM LFB ERROR FOR RXZ PISTON ,I5,5E18.11)
002561      GO TO 141
002562      145 RXP=1./(SOL(13,I)*SOL(13,I))*RXZDV*RXZDV*(SOL(13,I)-RZV)
002571      RZF=EQ(4)-RXP+ FPO
002574      GO TO 146
002575      142 ALB=SQRT((EQ(4) -FPO)*(SOL(13,I)-RZV))
002606      BLB=ALB
002607      GO TO 120
002607      900 FORMAT (12A6)
002607      901 FORMAT (12I5)
002607      902 FORMAT (4E18.11)
002607      903 FORMAT (2E18.11,2I5)
002607      904 FORMAT (80H1 A SIN ONE DIMENSIONAL REACTIVE HYDRODYNAMIC CALCULAT
ION IN SLAB GEOMETRY FOR ,/2X,12A6)
002607      905 FORMAT (87H1 A SIN ONE DIMENSIONAL REACTIVE HYDRODYNAMIC CALCULAT
ION IN CYLINDRICAL GEOMETRY FOR ,/2X,12A6)
002607      906 FORMAT (85H1 A SIN ONE DIMENSIONAL REACTIVE HYDRODYNAMIC CALCULAT
ION IN SPHERICAL GEOMETRY FOR ,/2X,12A6)
002607      907 FORMAT (//,32H THE NUMBER OF COMPONENTS IS ,I5)
002607      908 FORMAT (//,44H THE TOTAL NUMBER OF SPACE INCREMENTS IS ,I5)
002607      909 FORMAT (//,35H THE LEFT BOUNDARY IS A CONTINUUM)
002607      910 FORMAT (//,34H THE LEFT BOUNDARY IS A FREE SURFACE)
002607      911 FORMAT (//,59H THE LEFT BOUNDARY IS A PISTON WITH INITIAL VELOCI
TY OF ,E10.3,24H AND FINAL VELOCITY OF ,E10.3,/10X,23HWHEN W>3
2IS LESS THAN ,E10.3, 6H WITH ,I5,44H CELLS INITIALLY AND ADDING 0
3N A CELL EVERY ,I5, 7H CYCLES)
002607      912 FORMAT (//,49H THE LEFT BOUNDARY IS A PISTON WITH VELOCITY = ,

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$1E10.3,1H+1E10.3,6H$ (TIME),/,10X, 5HWITH ,I5,44H CELLS INITIALLY AND  
 2 ADDING ON A CELL EVERY ,I5, 7H CYCLES)  
 002607 913 FORMAT (//,36H THE RIGHT BOUNDARY IS A CONTINUUM)  
 002607 914 FORMAT (//,39H THE RIGHT BOUNDARY IS A FREE SURFACE)  
 002607 915 FORMAT (//,60H THE RIGHT BOUNDARY IS A PISTON WITH INITIAL VELOC  
     ITY OF ,1PE10.3,24H AND FINAL VELOCITY OF ,1PE10.3,/,10X,23HWHEN  
     2 W+3 IS LESS THAN ,1PE10.3, 6H WITH ,I5,44H CELLS INITIALLY AND A  
     3DDING ON A CELL EVERY ,I5, 7H CYCLES)  
 002607 916 FORMAT (//,50H THE RIGHT BOUNDARY IS A PISTON WITH VELOCITY = ,  
     11PE10.3,1H+1PE10.3,6H(TIME),/,10X, 5HWITH ,I5,44H CELLS INITIALLY  
     2 AND ADDING ON A CELL EVERY ,I5, 7H CYCLES)  
 002607 917 FORMAT (///,30X,33HTHE PARAMETERS FOR EACH COMPONENT)  
 002607 918 FORMAT (///,21H \* THE COMPONENT IS ,2A6,/,11H AND HAS ,I5,  
     122H SPACE INCREMENTS OF ,1PE10.3,34H CM EACH AND A TIME INCREMENT  
     2 OF ,1PE10.3,13H MICROSECONDS)  
 002607 919 FORMAT (//,80H IT IS TO BE CONSIDERED AS AN EXPLOSIVE AND WILL B  
     1E BURNED BY THE TECHNIQUE OF)  
 002607 921 FORMAT (//,53H THE ARRHENIUS RATE LAW WITH ACTIVATION ENERGY OF  
     1 ,1PE10.3,46H CALORIES PER MOLE AND A FREQUENCY FACTOR OF ,/,3X,  
     21PE10.3,16H PER MICROSECOND)  
 002607 922 FORMAT (//,45H THE CJ VOLUME BURN WITH A BURN VOLUME OF ,1PE10.  
     13,17H AND A MAX W OF ,1PE10.3)  
 002607 923 FORMAT (//,68H THE ARTIFICIAL PIC TYPE OF VISCOSITY IS USED WITH  
     1 A CONSTANT OF ,1PE10.3)  
 002607 924 FORMAT (//,74H THE ARTIFICIAL LANDSHOFF TYPE OF VISCOSITY IS USE  
     1D WITH A CONSTANT OF ,1PE10.3)  
 002607 925 FORMAT (//,76H THE TRUE FORM OF VISCOSITY IS USED WITH THE COEFF  
     ICIENT OF VISCOSITY OF ,1PE10.3)  
 002607 926 FORMAT (//,43H THE INITIAL CONDITIONS ARE A DENSITY OF ,1PE10.3,  
     123H GRAMS/CC, PRESSURE OF ,1PE10.3,26H MEGABARS, TEMPERATURE OF ,/  
     2,2X,1PE10.3,37H DEGREES KELVIN, INTERNAL ENERGY OF ,1PE10.3,33H M  
     3B-CC/GM, PARTICLE VELOCITY OF ,1PE10.3,16H CM/MICROSECOND,/,37H  
     4 AND MASS FRACTION OF THE SOLID OF ,1PE10.3)  
 002607 927 FORMAT (//129H THE HOM EQUATION OF STATE PARAMETERS FOR THE SOLI  
     1D C,S,VS,C1,S1,FS,GS,HS,IS,JS,GG,CV,V0,ALPHA,SPA,USP,T0,P0,Y0,MU,P  
     2LAP,SPP,VS2,/,,(6(2X,1PE18.11)))  
 002607 928 FORMAT (//108H THE HOM EQUATION OF STATE PARAMETERS FOR THE DETO  
     1NATION PRODUCTS A,B,C,D,E, K,L,M,N,O, Q,R,S,T,U,CVG,Z,/,,(6(2X,  
     21PE18.11)))  
 002607 929 FORMAT (//,57H A GAMMA LAW TAYLOR WAVE WITH DETONATION VELOCITY  
     1OF ,1PE10.3)  
 002607 930 FORMAT (//,77H THE LEFT BOUNDARY IS A STEADY STATE PISTON WITH A  
     1 DETONATION VELOCITY OF ,1PE10.3,17H SPIKE VOLUME OF ,1PE10.3,/  
     26H WITH ,I5,44H CELLS INITIALLY AND ADDING ON A CELL EVERY ,I5,  
     3 7H CYCLES)  
 002607 END

```

SUBROUTINE BURN (NMIN,NMAX)
C
C      BURN PERFORMS THE CHEMICAL REACTION ON CELLS WITH INDICES
C      NMIN TO NMAX
C
000004      COMMON CR(999),CRO(999),CU(999),CUO(999),CV(999),CVO(999),
1CM(999),CQ(999),ICF(999),CW(999),CWO(999),CT(999),CP(999),
2CS(999),CSZ(999),CI(999),CIO(999),LABEL(12)
000004      COMMON /MISC/ TTIME,DELT,ICYCL,PCNT,GCNT,DCNT,DINC,PINC,GINC,
1IALPH,HEATC,GASW,NCL,PTMIN,IPNT,IMC,IPR,ITR,IWR,IIR,IUR,IHC,ILB,
2IRB,WSW,PSMIN,WMAX,SMIN,ALB,BLB,ARB,BRB,NLI,NRI,NLINC,NRINC,
3NLNCNT,NRCNT,NLH,NRL,DX,KIND,RXZDV,RXZVS,FPO,FEO,RXZ
000004      COMMON /MATER/ E(10),GAS(17,10),IBRN(10),SOL(23,10),VCJ(10),
1VFACT(10),Z(10),NAM(2,10),DTIME(10),NOINC(10),IVIS(10),IEXP(10),
2NCOM
000004      DATA WMAX /.99/
C      SET W TO 0 IF LESS THAN GASW
000004      DATA GASW /+0.02/
000004      DO 10 I=NMIN,NMAX
000005      C      SKIP IF ALL BURNED
000005      IF (CW(I).EQ.0.) GO TO 10
000007      C      J IS INDEX OF COMPONENT
000007      KSP=ICF(I)/64
000012      J=ICF(I)-64*KSP
000016      C      CHECK FOR EXPLOSIVE OR GAS
000016      IF (IEXP(J).EQ.0) GO TO 10
000020      C      DETERMINE TYPE OF BURN
000020      IF (IBRN(J).NE.0) GO TO 1
000020      C      ARRHENIUS BURN
000020      IF E,Z, OR T LESS THAN 0.0001 DO NOT BURN
000021      IF(E(J).LT.0.0001) GO TO 2
000024      IF(Z(J).LT.0.0001) GO TO 2
000026      IF(CT(I).LT.0.0001) GO TO 2
000031      CW(I)=CWO(I)*(1.-DELT*Z(J)*EXP(-E(J)/(1.9865*CT(I))))
000050      GO TO 2
000050      C      CJ VOLUME BURN
000050      1 CW(I)=1.-(SOL(13,J)-CV(I))/(SOL(13,J)-VCJ(J))
000064      IF (CW(I).GT.CWO(I)) CW(I)=CWO(I)
000072      2 IF (CW(I).LT.GASW) CW(I)=0.
000077      10 CONTINUE
000102      RETURN
000102      END

```

```

SUBROUTINE ENERGY (NMIN,NMAX)
C
C ENERGY COMPUTES THE NEW INTERNAL ENERGY FOR CELLS WITH INDICES
C NMIN TO NMAX
C
000004      COMMON CR(999),CRO(999),CU(999),CUO(999),CV(999),CVO(999),
1CM(999),CQ(999),ICF(999),CW(999),CWO(999),CT(999),CP(999),
2CS(999),CSZ(999),CI(999),CIO(999),LABEL(12)
000004      COMMON /MISC/ TTIME,DELT,ICYCL,PCNT,GCNT,DCNT,DINC,PINC,GINC,
1IALPH,HEATC,GASW,NCL,PTMIN,IPNT,IMC,IPR,ITR,IWR,IIR,IUR,IHC,ILB,
2IRB,WSW,PSMIN,WMAX,SMIN,ALB,BLB,AR8,BRB,NLI,NRI,NLINC,NRINC,
3NLCNT,NRCNT,NLH,NRL,DX,KIND,RXZDV,RXZVS,FPO,FEO,RXZ
000004      COMMON /MATER/ E(10),GAS(17,10),IBRN(10),SOL(23,10),VCJ(10),
1VFACT(10),Z(10),NAM(2,10),DTIME(10),NOINC(10),IVIS(10),IEXP(10),
2NCOM
000004      IF (IALPH.EQ.0) GO TO 15
000005      DO 10 I=NMIN,NMAX
000006      CI(I)=CIO(I)+DELT/CM(I)*(((CM(I)*CP(I-1)+CM(I-1)*CP(I))/(
1(CM(I)+CM(I-1))+.5*(CQ(I)+CQ(I-1)))*CU(I)*CR(I)**IALPH-((CM(I+1)*
2CP(I)+CM(I)*CP(I+1))/(CM(I)+CM(I+1))+.5*(CQ(I)+CQ(I+1)))*CU(I+1)
3*CR(I+1)**IALPH)+((CUO(I+1)+CUO(I))*#2-(CU(I+1)+CU(I))**2)*.125
10 CONTINUE
000102      RETURN
000102      15 DO 20 I=NMIN,NMAX
000104      CI(I)=CIO(I)+DELT/CM(I)*(((CM(I)*CP(I-1)+CM(I-1)*CP(I))/(
1(CM(I)+CM(I-1))+.5*(CQ(I)+CQ(I-1)))*CU(I)-((CM(I+1)*
2CP(I)+CM(I)*CP(I+1))/(CM(I)+CM(I+1))+.5*(CQ(I)+CQ(I+1)))*CU(I+1)
3*((CUO(I+1)+CUO(I))*#2-(CU(I+1)+CU(I))**2)*.125
20 CONTINUE
000162      RETURN
000164      END
000164

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SUBROUTINE EAST (NMIN,NMAX)

C EQST DOES THE ELASTIC PLASTIC SPALLING EQUATION OF STATE
C CALCULATION FOR CELLS WITH INDICES NMIN TO NMAX
C
000004      COMMON CR(999),CRO(999),CU(999),CUO(999),CV(999),CVO(999),
1CM(999),CQ(999),ICF(999),CW(999),CWO(999),CT(999),CP(999),
2CS(999),CSZ(999),CI(999),CIO(999),LABEL(12)
000004      COMMON /MISC/ TTIME,DELT,ICYCL,PCNT,GCNT,DCNT,DINC,PINC,GINC,
1IALPH,HEATC,GASW,NCL,PTMIN,IPNT,IMC,IPR,ITR,IWR,IIR,IUR,IHC,ILB,
2IRB,WSW,PSMIN,WMAX,SMIN,ALB,BLB,ARB,BRB,NLI,NRI,NLINC,NRTNC,
3NLCNT,NRCNT,NLH,NRL,DX,KIND,RXZDV,RXZVS,FPO,FEO,RXZ
000004      COMMON /MATER/ E(10),GAS(17,10),IBRN(10),SOL(23,10),VCJ(10),
1VFACT(10),Z(10),NAM(2,10),DTIME(10),NOINC(10),IVIS(10),IEXP(10),
2NCOM
000004      DIMENSION EQ(5)
C      PSMIN = MINIMUM ELASTIC-PLASTIC PRESSURE
000004      DATA PSMIN /1.E-4/
000004      RFRNT=0.
000005      DO 20 I=NMIN,NMAX
C      KSP = 0 FOR NON SPALLED CELL
C          = 1 FOR SPALLED CELL
C          = 2 FOR INTERFACE CELL
000006      KSP=ICF(I)/64
C      J IS INDEX OF COMPONENT
000012      J=ICF(I)-64*KSP
000015      IF (KSP,EQ.2) RFRNT=CR(I)
000021      IF (CV(I).LT.SOL(13,J)) GO TO 1
000027      IF (KSP,NE.0) GO TO 11
000030      1 EQ(1)=CV(I)
000033      EQ(2)=CI(I)
C      CHECK FOR CJ EQUATION OF STATE
000035      IF (IBRN(J).NE.0) GO TO 9
000037      EQ(3)=CW(I)
000041      EQ(4)=0.
000042      IF (CV(I).GT.SOL(13,J)) EQ(4)=(CP(I))/ABS(CR(I)-RFRNT)
000056      CALL HOM (EQ,SOL(1,J),GAS(1,J),INDH)
000072      IF (INDH) 2,4,3
C      ERROR IN HOM
000073      2 PRINT 900,I,EQ
C      MAKE FAKE CALL TO TIME TO GET A LAST PRINT
000105      PCNT=1.
000106      GCNT=100.
000107      DCNT=100.
000110      ICYCL=ICYCL-1
000111      TTIME=TTIME-DELT
000113      CALL TIME
000117      STOP
000121      900 FORMAT (16H1 HOM ERROR .I5.5E18.11)
C      CELL SPALLED
000121      3 IF (ICF(I).LT.64) ICF(I)=ICF(I)+64
000127      RFRNT=CR(I)
000132      CP(I)=EQ(4)
000134      GO TO 11
C      REGULAR HOM EXIT
000134      4 CP(I)=EQ(4)
000137      IF (ABS(EQ(4)).LT.SOL(18,J)) CP(I)=SOL(18,J)
000151      CT(I)=EQ(5)
C      IF AN EXPLOSIVE OR GAS, SKIP ELASTIC-PLASTIC
000154      IF (IEXP(J).NE.0) GO TO 20
C      IF YO OR MU LESS THAN 0.0001 SKIP ELASTIC CALCULATION

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SUBROUTINE HETCON (NMIN,NMAX)
C
C   HETCON COMPUTES THE ADDITION TO THE INTERNAL ENERGY DUE TO
C   HEAT CONDUCTION FOR CELLS WITH INDICES NMIN TO NMAX
C
000004      COMMON CR(999),CRO(999),CU(999),CJO(999),CV(999),CVO(999),
1CM(999),CQ(999),ICF(999),CW(999),CWO(999),CT(999),CP(999),
2CS(999),CSZ(999),CI(999),CIO(999),LABEL(12)
000004      COMMON /MISC/ TTIME,DELT,ICYCL,PCNT,GCNT,DCNT,DINC,PINC,GINC,
1IALPH,HEATC,GASW,NCL,PTMIN,IPNT,IMC,IPR,IIR,IWR,IUR,IHC,ILB,
2IRR,WSW,PSMIN,WMAX,SMIN,ALB,BLB,ARB,BRB,NLI,NRI,NLINC,NRINC,
3NLCNT,NRCNT,NLH,NRL,DX,KIND,RXZDV,RXZVS,FPO,FEO,RXZ
000004      COMMON /MATER/ E(10),GAS(17,10),IBRN(10),SOL(23,10),VCJ(10),
1VFACT(10),Z(10),NAM(2,10),DTIME(10),NOINC(10),IVIS(10),IEXP(10),
2NCOM
000004      IF (IALPH.EQ.0) GO TO 15
000005      DO 10 I=NMIN,NMAX
000006      10 CI(I)=CI(I)+2.*HEATC*DELT/CM(I)*((CR(I+1)**IALPH)*(CT(I+1)-CT(I))
1/(CR(I+2)-CR(I))-(CR(I)**IALPH)*(CT(I)-CT(I-1))/(CR(I+1)-CR(I-1)))
000047      RETURN
000047      15 DO 20 I=NMIN,NMAX
000051      20 CI(I)=CI(I)+2.*HEATC*DELT/CM(I)*((CT(I+1)-CT(I))
1/(CR(I+2)-CR(I))-(CT(I)-CT(I-1))/(CR(I+1)-CR(I-1)))
000077      RETURN
000077      END

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SUBROUTINE RADIUS (NMIN,NMAX)
C   RADIUS COMPUTES THE CHANGES IN THE R COORDINATE IN A TIME STEP
C   FOR CELLS WITH INDICES NMIN TO NMAX
C
000004      COMMON CR(999),CRO(999),CU(999),CU0(999),CV(999),CV0(999),
1CM(999),CQ(999),ICF(999),CW(999),CW0(999),CT(999),CP(999),
2CS(999),CSZ(999),CI(999),CIO(999),LABEL(12)
000004      COMMON /MISC/ TTIME,DELT,ICYCL,PCNT,GCNT,DCNT,DINC,PINC,GINC,
1IALPH,HEATC,GASW,NCL,PTMIN,IPNT,IMC,IPR,ITR,IWR,IIR,IUR,IHC,ILB,
2IRB,WSW,PSMIN,WMAX,SMIN,ALB,BLB,ARB,BRB,NLI,NRI,NLINC,NRINC,
3NL_CNT,NRCNT,NLH,NRL,DX,KIND,RXZDV,RXZVS,FPO,FE0,RXZ
000004      COMMON /MATER/ E(10),GAS(17,10),IBRN(10),SOL(23,10),VCJ(10),
1VFACT(10),Z(10),NAM(2,10),DTIME(10),NOINC(10),IVIS(10),IEXP(10),
2NCOM
000004      DO 10 I=NMIN,NMAX
000005 10 CR(I)=CRO(I)+CU(I)*DELT
000014      RETURN
000014      END

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SUBROUTINE STRESS (NMIN,NMAX)
C
C   STRESS CALCULATES THE CHANGE IN THE STRESS DEVIATOR FOR CELLS
C   WITH INDICES NMIN TO NMAX
C
000004      COMMON CR(999),CRO(999),CU(999),CUO(999),CV(999),CVO(999),
1CM(999),CQ(999),ICF(999),CW(999),CWO(999),CT(999),CP(999),
2CS(999),CSZ(999),CI(999),CIO(999),LABEL(12)
000004      COMMON /MISC/ TTIME,DELT,ICYCL,PCNT,GCNT,DCNT,DINC,PINC,GINC,
1IALPH,HEATC,GASW,NCL,PTMIN,IPNT,IMC,IPR,IIR,IWR,IUR,IHC,ILB,
2IRB,WSW,PSMIN,WMAX,SMIN,ALB,BL8,ARB,BRB,NLI,NRI,NLINC,NRINC,
3NLINC,NRCNT,NLH,NRL,DX,KIND
000004      COMMON /MATER/ E(10),GAS(17,10),IBRN(10),SOL(23,10),VCJ(10),
1VFAC(10),Z(10),NAM(2,10),DTIME(10),NOINC(10),IVIS(10),IEXP(10),
2NCOM
C   CHANGE IN S MUST BE GREATER THAN SMIN BEFORE AFFECTING ANYTHING
000004      DATA SMIN /1.E-9/
000004      DO 10 I=NMIN,NMAX
000005      KSP=ICF(I)/64
C   J IS INDEX OF COMPONENT
000011      J=ICF(I)-64*KSP
C   IF YO OR MU LESS THAN 0.0001 SKIP ELASTIC CALCULATION
000014      IF(SOL(19,J).LT.0.0001) GO TO 10
000021      IF(SOL(20,J).LT.0.0001) GO TO 10
000024      DELS=2.*SOL(20,J)*((CU(I)-CU(I+1))*DELT/(CR(I+1)-CR(I))
1+.6666666667*(CV(I)-CVO(I))/(CV(I)+CVO(I)))
000047      IF (ABS(DELS).LT.SMIN) DELS=0.
000053      CS(I)=CS(I) + DELS
000057      IF (IALPH.EQ.1) GO TO 20
000061      GO TO 10
C   CALCULATE CSZ
000061      20 DELS = SOL(20,J)*1.33333334*(CV(I)-CVO(I))/(CV(I)+CVO(I))
000074      IF (ABS(DELS).LT.SMIN) DELS = 0.
000100      CSZ(I) = CSZ(I) + DELS
000104      10 CONTINUE
000107      RETURN
000107      END

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      SUBROUTINE TIME
C   TIME INCREMENTS THE TIME FOR EACH CYCLE AND DOES THE
C   PRINTING AND GRAPHING WHEN NECESSARY
C
000002      COMMON CR(999),CRO(999),CU(999),CUO(999),CV(999),CVO(999),
1CM(999),CQ(999),ICF(999),CW(999),CWO(999),CT(999),CP(999),
2CS(999),CSZ(999),CI(999),CIO(999),LABEL(12)
000002      COMMON /MISC/ TTIME,DELT,ICYCL,PCNT,GCNT,DCNT,DINC,PINC,GINC,
1ALPH,HEATC,GASW,NCL,PTMIN,IPNT,IMC,IPR,ITR,IWR,IIR,IUR,IHC,ILB,
2IRB,WSW,PSMIN,WMAX,SMIN,ALB,BLB,ARB,BRB,NLI,NRI,NLINC,NRINC,
3NLCNT,NRCNT,NLH,NRL,DX,KINU,RXZDV,RXZVS,FPO,FEO,RXZ
000002      COMMON /MATER/ E(10),GAS(17,10),IBRN(10),SOL(23,10),VCJ(10),
1VFACT(10),Z(10),NAM(2,10),DTIME(10),NOINC(10),IVIS(10),IEXP(10),
2NCOM
000002      DIMENSION ICHAR(2),TKE(10),TIE(10)
C   PLOT CHARACTERS    1.   .   2.   X
000002      DATA ICHAR(1) /052/
000002      DATA ICHAR(2) /067/
C   THE PRESSURE OF ONE CELL OF A COMPONENT MUST BE GREATER THAN
C   PTMIN TO USE THAT COMPONENTS DELTA T
000002      DATA PTMIN /1.E-05/
000002      DATA ICYCL /0/
000002      DATA PCNT /1./
000002      DATA GCNT /1./
000002      DATA DCNT /100./
C   INCREMENT TIME AND CYCLE NUMBER
000002      ICYCL=ICYCL+1
000004      TTIME=TTIME+DELT
000006      NRCNT=NRCNT-1
000007      NLCNT=NLCNT-1
C   SEE IF WE NEED TO ADD ON CELLS FROM LEFT
000010      IF (NLCNT.GT.0) GO TO 4
000012      C   YES   ADD ON A CELL AND SET COUNT
000013      NLH=NLH+1
000013      NLCNT=NLCNT
C   SEE IF WE NEED TO ADD ON CELLS FROM RIGHT
000014      4 IF (NRCNT.GT.0) GO TO 5
000014      C   YES   ADD ON A CELL AND SET COUNT
000017      NRL=NRL-1
000020      NRCNT=NRINC
C   CHECK IF ALL CELLS ARE IN THE CALCULATION
000021      5 IF (NRL.GT.NLH+1) GO TO 6
000021      C   YES   SET NLI,NRI,NLH, AND COUNTS ACCORDINGLY
000026      NLH=NCL+1
000027      NLI=1
000030      NRI=0
000031      NLCNT=100000
000032      NRCNT=100000
000033      GO TO 7
C   CHECK IF ALL CELLS ARE IN THE CALCULATION
000033      6 IF (NLH.LT.NCL) GO TO 7
000033      C   YES   SET NLI,NRI,NLH, AND COUNTS ACCORDINGLY
000035      NRCNT=100000
000037      NLCNT=100000
000040      NLH=NCL+1
000041      NRI=0
000042      NLI=1
C   DETERMINE DELT FOR NEXT CYCLE
000043      7 K=1
C   SAVE DELTA T FOR PRINT OUT

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000044      SVDEL=DELT
000046      DO 10 I=1,NCOM
000047      N=N0INC(I)
000051      DO 8 J=1,N
000053      IF (CP(K+J).GT.PTMIN) GO TO 9
000060      8 CONTINUE
000062      GO TO 10
000062      9 IF (DELT.GT.DTIME(I)) DELT=DTIME(I)
000067      10 K=K+N
C      DECREMENT COUNTS
000073      PCNT=PCNT-1.
000075      GCNT=GCNT-1.
000077      DCNT=DCNT-1.
000100      IF (PCNT.GT.0.) GO TO 20
000102      PCNT=PINC
000103      PRINT 900,ICYCL,TTIME,LABEL
000114      PRINT 906,SVDEL,NLH,NRL
000126      LIN=56
000127      K=1
000130      DO 15 I=1,NCOM
000132      N=N0INC(I)
000134      TKE(I)=0.
000136      TIE(I)=0.
000137      L=K
000141      DO 11 J=1,N
000142      TKE(I)=TKE(I)+CM(L)*CU(L+1)*CU(L+1)
000150      TIE(I)=TIE(I)+CM(L)*CI(L)
000154      L=L+1
000155      11 CONTINUE
000160      TKE(I)=TKE(I)*.50036186
000163      IF (LIN.LT.6) GO TO 12
000165      PRINT 901,NAM(1,I),NAM(2,I),TKE(I),TIE(I)
000206      LIN=LIN-5
000210      GO TO 13
000210      12 PRINT 902,NAM(1,I),NAM(2+I),TKE(I),TIE(I)
000232      PRINT 903
000236      LIN=55
000237      13 IF (I.EQ.1) PRINT 903
000245      IF (I.EQ.1) N=N+1
000250      IF (I.EQ.NCOM) N=N+1
000253      EINO=-1.
000255      DO 14 J=1,N
000256      IF (CI(K).EQ.EINO) GO TO 14
000261      IFLG=ICF(K)/64
000264      IF (LIN.EQ.0) PRINT 904
000271      IF (LIN.EQ.0) LIN=58
000273      PRINT 905,K,CR(K),CU(K),CV(K),CI(K),CP(K),CT(K),CW(K),CQ(K),CM(K),
1CS(K),CSZ(K),IFLG
000344      LIN=LIN-1
000346      EINO=CI(K)
000350
000354      14 K=K+1
000357      15 CONTINUE
      IF (IMC.EQ.0) GO TO 20
*****4020 OUTPUT BELOW*****
*****4020 OUTPUT BELOW*****
000360      WRITE (12,900) ICYCL,TTIME,LABEL
000371      WRITE (12,906) SVDEL,NLH,NRL
000403      LIN=56
000404      K=1
000405      DO 19 I=1,NCOM
000407      EINO=-1.

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000411      N=NOINC(I)
000413      IF (LIN.LT.6) GO TO 16
000415      WRITE (12,901) NAM(1,I),NAM(2+I),TKE(I),TIE(I)
000436      LIN=LIN-5
000440      GO TO 17
000440      16 WRITE (12,902) NAM(1,I),NAM(2+I),TKE(I),TIE(I)
000462      WRITE (12,903)
000466      LIN=55
000467      17 IF (I.EQ.1) WRITE (12,903)
000475      IF (I.EQ.1) N=N+1
000500      IF (I.EQ.NCOM) N=N+1
000503      DO 18 J=1,N
000505      IF (CI(K).EQ.EINO) GO TO 18
000510      IFLG=ICF(K)/64
000513      IF (LIN.EQ.0) WRITE (12,904)
000520      IF (LIN.EQ.0) LIN=58
000522      WRITE (12,905) K,CR(K),CU(K),CV(K),CI(K),CP(K),CT(K),CW(K),CQ(K),
     1CM(K),CS(K),CSZ(K),IFLG
000573      LIN=LIN-1
000575      EINO=CI(K)
000577      18 K=K+1
000603      19 CONTINUE
C          **** OUTPUT ABOVE ****
C          4020 OUTPUT ABOVE
C          **** OUTPUT BELOW ****
C          4020 OUTPUT BELOW
C          **** OUTPUT BELOW ****
000606      20 IF (GCNT.GT.0.) GO TO 50
000611      GCNT=GINC
000612      IF (IMC.EQ.0) GO TO 50
C          **** OUTPUT BELOW ****
C          **** OUTPUT BELOW ****
000613      IF (IPR.EQ.0) GO TO 32
C          GRAPH PRESSURE VS RADIUS
000614      CALL ADV(1)
000615      CALL DGA (123,1023,0,900.0,CR(NCL+1),.90,--,1)
000625      CALL DLNLN (10,10)
000627      CALL SLLIN (10,2)
000631      CALL SBLIN (10,3)
000633      J=1
000634      K=2
000635      DO 31 I=1,NCOM
000637      N=NOINC(I)
000641      CALL PLOT (N,CR(K),1,CP(K)+1,ICHAR(J)+1)
000652      J=3-J
000654      K=K+N
000655      31 CONTINUE
000660      CALL LINCNT (60)
000661      WRITE (12,910) LABEL
000667      WRITE (12,911) TTIME,ICYCL
000677      32 IF (ITR.EQ.0) GO TO 34
C          GRAPH TEMPERATURE VS RADIUS
000700      CALL ADV(1)
000702      CALL DGA (123,1023,0,900.0,CR(NCL+1),5000.0,0.)
000712      CALL DLNLN (10,10)
000714      CALL SLLIN (10,0)
000716      CALL SBLIN (10,3)
000720      J=1
000721      K=2
000722      DO 33 I=1,NCOM
000724      N=NOINC(I)
000726      CALL PLOT (N,CR(K),1,CT(K)+1,ICHAR(J)+1)
000737      J=3-J

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000741      K=N
000742      33 CONTINUE
000745      CALL LINCNT (60)
000746      WRITE (12,910) LABEL
000754      WRITE (12,912) TTIME,ICYCL
000764      34 IF (IWR,EQ.0) GO TO 36
C      GRAPH MASS FRACTION VS RADIUS
000765      CALL ADV(1)
000767      CALL DGA (123,1023,0,900.0,,CR(NCL+1),1.,0.)
000777      CALL DLNLN (10,10)
001001      CALL SLLIN (10,2)
001003      CALL SBLIN (10,3)
001005      J=1
001006      K=2
001007      DO 35 I=1,NCOM
001011      N=NOINC(I)
001013      CALL PLOT (N,CR(K),1,CW(K)+1,ICHAR(J)+1)
001024      J=3-J
001026      K=N
001027      35 CONTINUE
001032      CALL LINCNT (60)
001033      WRITE (12,910) LABEL
001041      WRITE (12,913) TTIME,ICYCL
001051      36 IF (IIR,EQ.0) GO TO 38
C      GRAPH VOLUME VS RADIUS
001052      CALL ADV(1)
001054      CALL DGA (123,1023,0,900.0,,CR(NCL+1),2.,0.)
001064      CALL DLNLN (10,10)
001066      CALL SLLIN (10,3)
001070      CALL SBLIN (10,3)
001072      J=1
001073      K=2
001074      DO 37 I=1,NCOM
001076      N=NOINC(I)
001100      CALL PLOT (N,CR(K),1,CV(K)+1,ICHAR(J)+1)
001111      J=3-J
001113      K=N
001114      37 CONTINUE
001117      CALL LINCNT (60)
001120      WRITE (12,910) LABEL
001126      WRITE (12,914) TTIME,ICYCL
001136      38 IF (IUR,EQ.0) GO TO 50
C      GRAPH VELOCITY VS RADIUS
001137      CALL ADV(1)
001141      CALL DGA (123,1023,0,900.0,,CR(NCL+1),1.0,-1.0)
001151      CALL DLNLN (10,10)
001153      CALL SLLIN (10,2)
001155      CALL SBLIN (10,3)
001157      J=1
001160      K=2
001161      DO 39 I=1,NCOM
001163      N=NOINC(I)
001165      CALL PLOT (N,CR(K),1,CU(K)+1,ICHAR(J)+1)
001176      J=3-J
001200      K=N
001201      39 CONTINUE
001204      CALL LINCNT (60)
001205      WRITE (12,910) LABEL
001213      WRITE (12,915) TTIME,ICYCL
*****4020 OUTPUT ABOVE*****
*****4020 OUTPUT ABOVE*****

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001223      50 IF (DCNT.GT.0.) RETURN
001225          DCNT=DINC
001227          WRITE (1) CRO,CUO,CWO,CSZ,CIO,CVO,ICF,CM,CQ,CT,CP,LABEL,DELT,HEATC,
1IALPH,TTIME,PINC,GINC,DINC,PCNT,GCNT,DCNT,E,GAS,IBRN,SOL,VCJ,
2VFACT,Z,NAM,DTIME,NOINC,NCOM,ICYCL,NCL,IPNT,IMC,IPR,ITR,IWR,IIR,
3IUR,IHC,ILB,IRB,ALB,BLB,ARB,BRB,WSW,NLI,NRI,NLINC,NRINC,NLCNT,
4NRNCNT,NLH,NRL,DX,IVIS,IEXP,KIND,CR,CI,CW,CV,CU,CS,RXZDV,RXZVS,
5RXZ,FPO,FE0
001454      PRINT 916,ICYCL
001462      RETURN
001463 900 FORMAT (12H1 AT CYCLE ,I5+13H THE TIME IS ,1PE11.4+18H MICROSECON
1DS FOR ,12A6)
001463 901 FORMAT (//,20H THE COMPONENT IS ,2A6+26H WITH A KINETIC ENERGY 0
1F ,1PE11.4+27H AND AN INTERNAL ENERGY OF ,1PE11.4,/)
001463 902 FORMAT (20H1 THE COMPONENT IS ,2A6+26H WITH A KINETIC ENERGY 0
1F ,1PE11.4+27H AND AN INTERNAL ENERGY OF ,1PE11.4,/)
001463 903 FORMAT (129H CELL RADIUS VEL VOLUME ENERGY
1 PRESS TEMP MASS F VISC MASS X,Z ST
2RESS FLAG)
001463 904 FORMAT (129H1CELL RADIUS VEL VOLUME ENERGY
1 PRESS TEMP MASS F VISC MASS X,Z ST
2RESS FLAG)
001463 905 FORMAT (I5,9(X,1PE11.4),X,2(3PF6.3),X,02)
001463 906 FORMAT (14H DELTA T IS ,1PE10.3,25H WITH LEFT CELL INDEX OF ,I5,
125H AND RIGHT CELL INDEX OF ,I5)
001463 910 FORMAT (10X,12A6)
001463 911 FORMAT (//,10X,38HPRESSURE (MEGABARS) VS RADIUS (CM) AT ,1PE10.3+
131H MICROSECONDS AND CYCLE NUMBER ,I5)
001463 912 FORMAT (//,10X,43HTEMPERATURE (DEG KELVIN) VS RADIUS (CM) AT ,
11PE10.3,31H MICROSECONDS AND CYCLE NUMBER ,I5)
001463 913 FORMAT (//,10X,41HMASS FRACTION OF SOLID VS RADIUS (CM) AT ,1PE10.
13,31H MICROSECONDS AND CYCLE NUMBER ,I5)
001463 914 FORMAT (//,10X,45H SPECIFIC VOLUME (CC/GM) VS RADIUS (CM) AT ,
11PF10.3,31H MICROSECONDS AND CYCLE NUMBER ,I5)
001463 915 FORMAT (//,10X,46HPARTICLE VELOCITY (CM/MSEC) VS RADIUS (CM) AT ,
11PE10.3,31H MICROSECONDS AND CYCLE NUMBER ,I5)
001463 916 FORMAT (///,10X,19HTAPE DUMP AT CYCLE ,I5)
001463      END

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SUBROUTINE UPDATE (NMIN,NMAX)
C
C      UPDATE MOVES THE NEW QUANTIES TO THE OLD TIME STEP QUANTIES
C
000004    COMMON CR(999),CRO(999),CU(999),CUD(999),CV(999),CVO(999),
1CM(999),CQ(999),ICF(999),CW(999),CWO(999),CT(999),CP(999),
2CS(999),CSZ(999),CI(999),CIO(999),LABEL(12)
000004    COMMON /MISC/ TTIME,DELT,ICYCL,PCNT,GCNT,DCNT,DINC,PINC,GINC,
1IALPH,HEATC,GASW,NCL,PTMIN,IPNT,IMC,IPR,IIR,IWR,IUR,IHC,ILB,
2IRR,WSW,PSMIN,WMAX,SMIN,ALB,BLB,ARB,BRB,NLI,NRI,NLINC,NRINC,
3NLCNT,NRCNT,NLH,NRL,DX,KIN0,RXZDV,RXZVS,FPO,FEO,RXZ
000004    COMMON /MATER/ E(10),GAS(17,10),IBRN(10),SOL(23,10),VCJ(10),
1VFACT(10),Z(10),NAM(2,10),DTIME(10),NOINC(10),IVIS(10),IEXP(10),
2NCOM
000004    DO 10 I=NMIN,NMAX
000005    CRO(I)=CR(I)
000010    CUD(I)=CU(I)
000012    CVO(I)=CV(I)
000015    CWO(I)=CW(I)
000017    10 CIO(I)=CI(I)
000024    RETURN
000024    END

```

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      SUBROUTINE VELOC (NMIN,NMAX)

C   VELOC CALCULATES THE NEW VELOCITY AT THE NEXT TIME STEP FOR
C   CELLS WITH INDICES FROM NMIN TO NMAX

000004      COMMON CR(999),CRO(999),CU(999),CU0(999),CV(999),CVO(999),
1CM(999),CQ(999),ICF(999),CW(999),CWO(999),CT(999),CP(999),
2CS(999),CSZ(999),CI(999),CIO(999),LABEL(12)
000004      COMMON /MISC/ TTIME,DELT,ICYCL,PCNT,GCNT,DCNT,DINC,PINC,GINC,
1IALPH,HEATC,GASW,NCL,PTMIN,IPNT,IMC,IPR,ITR,IWR,IIR,IUR,IHC,ILB,
2IRB,WSW,PSMIN,WMAX,SMIN,ALB,BLB,ARB,BRB,NLI,NRI,NLINC,NRINC,
3NLCNT,NRCNT,NLH,NRL,DX,KIND,RXZDV,RXZVS,FPO,FEO,RXZ
000004      COMMON /MATER/ E(10),GAS(17,10),IBRN(10),SOL(23,10),VCJ(10),
1VFACT(10),Z(10),NAM(2,10),DTIME(10),NOINC(10),IVIS(10),IEXP(10),
2NCOM
000004      IF (IALPH.EQ.0) GO TO 15
000005      DO 10 I=NMIN,NMAX
C       J IS INDEX OF COMPONENT
000006      KSP=ICF(I)/64
000012      J = ICF(I)-64*KSP
000015      CU(I)=CU0(I)+2.*DELT*(CRO(I)*IALPH)/(CM(I-1)+CM(I))*(CP(I-1)
1-CP(I)+CQ(I-1)-CQ(I))
C       IF YO OR MU LESS THAN 0.0001 SKIP ELASTIC CALCULATION
000040      IF(SOL(19,J).LT.0.0001) GO TO 10
000045      IF(SOL(20,J).LT.0.0001) GO TO 10
000050      IF (CRO(I).EQ.0.) GO TO 10
000052      IF (IALPH.EQ.1) GO TO 50
C       VELOCITY CALCULATION FOR ELASTIC SPHERE
000054      CU(I)=CU(I)-0.75*(CS(I)+CS(I-1))*(CVO(I)+CVO(I-1))*DELT/CRO(I)
000067      C       VELOCITY CALCULATION FOR ELASTIC CYLINDER
000067      50 CU(I)=CU(I)-(CS(I)+CS(I-1)+0.5*(CSZ(I)+CSZ(I-1)))*0.5*(CVO(I)-
1CVO(I-1))*DELT/CRO(I)
000107      10 CONTINUE
000112      RETURN
000112      15 DO 20 I=NMIN,NMAX
000114      20 CU(I)=CU(I)+2.*DELT/(CM(I-1)+CM(I))*(CP(I-1)
1-CP(I)+CQ(I-1)-CQ(I))
000135      RETURN
000135      END

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      SUBROUTINE VISCOS (NMIN,NMAX)
C
C   VISCOS COMPUTES THE VISCOSITY IN EITHER THE PIC, LANDSHOFF, OR
C   REAL FORM FOR CELLS WITH INDICES NMIN TO NMAX
C
000004      COMMON CR(999),CRO(999),CU(999),CUO(999),CV(999),CV0(999),
1CM(999),CQ(999),ICF(999),CW(999),CWO(999),CT(999),CP(999),
2CS(999),CSZ(999),CI(999),CIO(999),LABEL(12)
000004      COMMON /MISC/ TTIME,DELT,ICYCL,PCNT,GCNT,DCNT,DINC,PINC,GINC,
1IALPH,HEATC,GASW,NCL,PTMIN,IPNT,IMC,IPR,ITR,IWR,IIR,IUR,IHC,ILB,
2IRR,WSW,PSMIN,WMAX,SMIN,ALB,BLB,ARB,BRB,NLI,NRI,NLINC,NRINC,
3NLNCNT,NRCNT,NLH,NRL,DX,KIND,RXZDV,RXZVS,FPO,FE0,RXZ
000004      COMMON /MATER/ E(10),GAS(17,10),IBRN(10),SOL(23,10),VCJ(10),
1VFACT(10),Z(10),NAM(2,10),DTIME(10),NOINC(10),IVIS(10),IEXP(10),
2NCOM
000004      DO 10 I=NMIN,NMAX
000005      UT=CU(I)-CU(I+1)
000010      C J IS INDEX OF COMPONENT
000013      KSP=ICF(I)/64
000013      J=ICF(I)-64*KSP
000017      C CHECK FOR REAL FORM
000017      IF (IVIS(J).EQ.2) GO TO 2
000022      CQ(I)=0.
000024      IF (UT.LE.0.) GO TO 10
000025      C CHECK FOR LANDSHOFF FORM
000025      IF (IVIS(J).EQ.1) GO TO 1
000030      C PIC FORM
000030      CQ(I)=ABS(VFACT(J)*.5*(CU(I)+CU(I+1))*UT/CV(I))
000042      GO TO 10
000042      C LANDSHOFF FORM
000042      1 CQ(I)=VFACT(J)*UT/CV(I)
000050      GO TO 10
000050      C REAL FORM
000050      2 CQ(I)=1.3333*VFACT(J)*UT/(CV(I)*CM(I))
10 CONTINUE
000061      RETURN
000064      END
000064

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C          SUBROUTINE VOLUM (NMIN,NMAX)
C          VOLUM FINDS THE SPECIFIC VOLUME OF CELLS WITH INDICES NMIN TO NMAX
000004      COMMON CR(999),CRO(999),CU(999),CU0(999),CV(999),CVO(999),
1CM(999),CQ(999),ICF(999),CW(999),CWO(999),CT(999),CP(999),
2CS(999),CSZ(999),CI(999),CIO(999),LABEL(12)
000004      COMMON /MISC/ TTIME,DELT,ICYCL,PCNT,GCNT,DCNT,DINC,PINC,GINC,
1IALPH,HEATC,GASW,NCL,PTMIN,IPNT,IMC,IPR,ITR,IWR,IIR,IUR,IHC,ILB,
2IRB,WSW,PSMIN,WMAX,SMIN,ALB,BLB,ARB,BRB,NLI,NRI,NLINC,NRINC,
3NLCNT,NRCNT,NLH,NRL,DX,KIND,RXZDV,RXZVS,FPO,FEO,RXZ
000004      COMMON /MATER/ E(10),GAS(17,10),IBRN(10),SOL(23,10),VCJ(10),
1VFACT(10),Z(10),NAM(2,10),DTIME(10),NOINC(10),IVIS(10),IEXP(10),
2NCOM
000004      DO 10 I=NMIN,NMAX
000005      10 CV(I)=((CR(I+1)+CR(I))*.5)**IALPH*(CR(I+1)-CR(I))/CM(I)
000024      RETURN
000024      END

```

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SUBROUTINE HOM (V,S,G,IND)
C
C HOM CALCULATES THE EQUATION OF STATE FOR A SOLID, GAS, OR
C SOLID-GAS MIXTURE.
C
C THE PARAMETERS ARE
C V AN ARRAY OF DIMENSION 5
C   V(1) SPECIFIC VOLUME      INPUT
C   V(2) INTERNAL ENERGY     INPUT
C   V(3) MASS FRACTION       INPUT
C   V(4) -ABS(DP/DX)         INPUT
C IF V(4) IS .GE.0 NO SPALLING CALCULATION IS DONE FOR A PURE
C SOLID
C   V(4) PRESSURE            OUTPUT
C   V(5) TEMPERATURE          OUTPUT
C S AN ARRAY OF DIMENSION 18 CONTAINING THE PARAMETERS FOR THE
C SOLID EQUATION OF STATE
C   S(1) C
C   S(2) S
C   S(3) VSW    VOLUME TO SWITCH TO SECOND US-UP FIT
C   S(4) C1
C   S(5) S1
C   S(6) F
C   S(7) G
C   S(8) H
C   S(9) I
C   S(10) J
C   S(11) GAMMA
C   S(12) CV
C   S(13) V0    INITIAL VOLUME
C   S(14) ALPHA
C   S(15) SPALL A
C   S(16) ULTIMATE SPALL PRESSURE
C   S(17) T0    INITIAL TEMPERATURE
C   S(18) P0    INITIAL PRESSURE
C   S(22) IS SPALL INTERFACE PRESSURE
C   S(23) IS MIN V FOR TWO PHASE FE EQUATION OF STATE
C G AN ARRAY OF DIMENSION 17 CONTAINING THE PARAMETERS FOR THE
C GAS EQUATION OF STATE
C   G(1) A
C   G(2) B
C   G(3) C
C   G(4) D
C   G(5) E
C   G(6) K
C   G(7) L
C   G(8) M
C   G(9) N
C   G(10) O
C   G(11) Q
C   G(12) R
C   G(13) S
C   G(14) T
C   G(15) U
C   G(16) CV
C   G(17) Z
C IND   OUTPUT INDICATOR
C SET TO 0 FOR NORMAL EXIT
C SET TO 1 FOR SPALLED SOLID
C SET TO -1 FOR HOM ERROR IN ITERATION
C DIMENSION V(5),S(23)*G(17)*VIT(10)
000006

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000006      DATA GASW /.01/
000006      DATA SOLW /.999/
000006      DATA SPMIN/5.0E-3/
000006      DATA VGSS /.9/
000006      DATA VIT(3) /1.E-5/
000006      DATA VIT(10) /0./
000006      IND=0
000006      IF (V(3).GT.SOLW) GO TO 10
000012      IF (V(3).LT.GASW) GO TO 110
000014      GO TO 210
C   EQUATION OF STATE FOR SOLID ONLY
000014      10 IF (V(1).GT.S(13)) GO TO 50
C   FOR TWO PHASE FE TYPE EQUATION OF STATE
000020      IF(V(1).GT.S(3)) GO TO 11
000023      IF(V(1).LT.S(23)) GO TO 45
000024      V(1)=S(23)
000026      GO TO 45
000026      11 C1=S(1)
000027      S1=S(2)
000031      20 VOMV=S(13)-V(1)
000033      HP=(C1/(S(13)-S1)*VOMV)*#2)*VOMV
000040      HE=HP*VOMV*.5
000042      V(4)=HP+(V(2)-HE)*S(11)/V(1)
C   IF NO HEAT CAPACITY SKIP TEMP CALCULATION
000047      IF (S(12)) 21,22,21
000050      21 ALNV=ALOG(V(1))
000055      V(5)=(V(2)-HE)*23890./S(12)+EXP(S(6)+ALNV*(S(7)+ALNV*(S(8)+ALNV*
1(S(9)+ALNV*S(10)))))
000077      22 RETURN
C   SWITCH TO SECOND US.UP FIT
000100      45 C1=S(4)
000102      S1=S(5)
000103      GO TO 20
C   SPALLING SOLID EQUATION OF STATE
000104      50 DPDX=V(4)
C   IF ALPHA IS ZERO SET P=P0 AND DO NOT SPALL
000106      IF (S(14)) 51,51,52
000107      51 V(4)=S(18)
000111      V(5)=S(17)
000112      RETURN
000113      52 V(4)=(S(11)*(V(2)+(1.-V(1)/S(13)))*S(12)*1.39528394E-5/S(14)))/V(1)
000125      V(5)=V(2)*23890./S(12)+S(17)
000131      IF (DPDX.GE.0.) RETURN
C   IF SPA LESS THAN / 0.0001 DO NOT SPALL
000134      IF (S(15) .LT.0.0001) RETURN
000137      T=S(15)*SQRT(-DPDX)
000147      SPLP=-T
000150      IF (T.GT.S(16)) SPLP=-S(16)
000154      IF (T.LT.SPMIN) SPLP=-SPMIN
000160      IF (V(4).GT.SPLP) RETURN
000163      V(4)=S(22)
C   SET IND FOR SPALLED SOLID
000165      IND=1
000166      RETURN
C   EQUATION OF STATE FOR GAS ONLY
000166      110 ALNV=ALOG(V(1))
000173      ALNPI=G(1)+ALNV*(G(2)+ALNV*(G(3)+ALNV*(G(4)+ALNV*G(5))))
000203      ALNII=G(6)+ALNPI*(G(7)+ALNPI*(G(8)+ALNPI*(G(9)+ALNPI*G(10))))
000214      ALNTI=G(11)+ALNV*(G(12)+ALNV*(G(13)+ALNV*(G(14)+ALNV*G(15))))
000225      EI=EXP(ALNII)-G(17)
000233      V(4)=EXP(ALNPI)*(EI-V(2))/V(1)*(G(12)+ALNV*(G(13)+G(14)+ALNV*(13+G(14)+ALNV*4.*G(15))))

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000257      V(5)=EXP(ALNTI)+(V(2)-EI)*23890./G(16)
000272      RETURN
C   EQUATION OF STATE FOR MIXTURE OF SOLID AND GAS
000272      210 OMW=1.-V(3)
000274      OMWR=1./OMW
000276      IF (V(1).LT.S(13)) GO TO 230
000300      WR=1./V(3)
000302      VIT(1)=(V(1)-V(3)*S(13)*VGSS)*OMWR
000307      VIT(2)=1.002
C   IBR=1 FOR ITERATION ON VG
000310      IBR=1
000311      215 CALL LFB (X,F,VIT)
000321      IF (VIT(10)) 900,260+220
000323      220 IF (X.LE.0.) GO TO 225
000325      VG=X
000326      VS=(V(1)-OMW*VG)*WR
000328      IF (VS.LE.0.) GO TO 225
000333      IF (VS.GT.S(13)) VS=S(13)
000337      GO TO 250
C   SET VS=VG=VOLUME WHEN GET IN TROUBLE
000340      225 VS=V(1)
000341      VG=V(1)
000342      X=V(1)
000343      GO TO 250
000344      230 VIT(1)=V(1)
000345      VIT(2)=.999
C   IBR=2 FOR ITERATION ON VS
000347      IBP=2
000350      235 CALL LFB (X,F,VIT)
000360      IF (VIT(10)) 900,260+240
000362      240 IF (X.LE.0.) GO TO 225
000364      IF (X.GT.S(13)) X=S(13)
000367      VS=X
000370      VG=(V(1)-V(3)*VS)*OMWR
000374      IF (VG.LE.0.) GO TO 225
C   CALCULATE TEMPERATURE/PRESSURE DIFFERENCE FOR MIXTURE ITERATION
000375      250 VOMV=S(13)-VS
000377      HP=((S(1)/(S(13)-S(2)*VOMV))**2)*VOMV
000404      HE=HP+.5*VOMV
000406      ALNV=ALOG(VS)
000412      HT=EXP(S(6)+ALNV*(S(7)+ALNV*(S(8)+ALNV*(S(9)+ALNV*S(10))))) )
000427      ALNV=ALOG(VG)
000434      ALNPI=G(1)+ALNV*(G(2)+ALNV*(G(3)+ALNV*(G(4)+ALNV*G(5)))) )
000444      EI=EXP(G(6)+ALNPI*(G(7)+ALNPI*(G(8)+ALNPI*(G(9)+ALNPI*G(10)))) )-
1G(17)
000463      PI=EXP(ALNPI)
000467      TI=EXP(G(11)+ALNV*(G(12)+ALNV*(G(13)+ALNV*(G(14)+ALNV*G(15))))) )
000504      BETER=- (G(12)+ALNV*(G(13)+G(13)+ALNV*(3.*G(14)+4.*ALNV*G(15)))) )
000515      TEMP=-G(16)*BETER/VG
000520      TEMP1=S(11)*S(12)/VS
000523      F=-(HT*TEMP1+TI*TEMP)*4.18585182E-5
000527      TEMP=TEMP+TEMP1
000531      VSTO=(S(12)-G(16))*V(3)*G(16)
000534      F=((OMW*G(16)*TI+V(3)*S(12)*HT)*4.18585182E-5+(EI-HE)*V(3)-EI-
1V(2))*TEMP/VSTO+F-PI+HP
000556      GO TO (215,235),IBR
C   HAVE FOUND A SOLUTION FOR THE MIXTURE
C   GET THE TEMPERATURE AND PRESSURE
000563      260 VARST=((((TI-HT)*G(16)*4.18585182E-5+V(2)*OMWR-EI)*S(12)+HE*G(16))-
1*OMW/VSTO)-HE
000600      V(4)=HP+VARST*S(11)/VS
000604      V(5)=HT+VARST*23890./S(12)

```

```
000610      RETURN  
000610      C   ERROR IN HOM ITERATION      SET IND TO -1  
000610      900 IND=-1  
000611      RETURN  
000612      END
```

```

        SURROUTINE LFB (XP,FP,TX)

C      TX(1)      INITIAL GUESS
C      TX(2)      RATIO TO GET SECOND POINT
C      TX(3)      ZERO DEFINITION
C      TX(10)     COUNT OF NUMBER OF ITERATIONS
C                  SET TO ZERO ON SOLUTION
C                  SET TO NEGATIVE OF COUNT ON ERROR
C      FP         =FUNCTION(XP)
C      WHEN A SOLUTION IS FOUND, XP IS THE ROOT
C
C      ERROR EXITS OCCUR FOR
C          1. TOO MANY ITERATIONS, .GT.CNTMAX
C          2. TWO SUCESSIVE XP S OR FP S ARE EQUAL

000005    DIMENSION TX(10)
000005    DATA CNTMAX /1000./
000005    IF (TX(10).LE.0.) GO TO 1
000006    TX(10)=TX(10)+1.
000011    IF (TX(10)-3.) 2,3,4
C      ENTRY FIRST TIME THROUGH
000014    1 TX(10)=1.
000016    IF (TX(1).EQ.0.) TX(1)=1.
000020    XP=TX(1)
C      GO GET F(XP)
000021    RETURN
C      ENTRY SECOND TIME THROUGH
000022    2 TX(9)=FP
000024    TX(8)=XP
000025    TX(5)=FP
000026    IF (ABS(FP).LT.TX(3)) GO TO 18
000030    XP=TX(1)+TX(2)
C      GO GET F(XP)
000031    RETURN
C      ENTRY THIRD TIME THROUGH
000032    3 TX(5)=FP
000034    TX(6)=XP
000035    TX(7)=FP
000036    IF (ABS(FP).LT.TX(3)) GO TO 18
000040    XP=TX(6)-TX(7)*(TX(6)-TX(8))/(TX(7)-TX(9))
C      GO GET F(XP)
000047    RETURN
C      ENTRY FOR FOURTH AND SUCCEEDING TIMES THROUGH
000050    4 IF (TX(10).GT.CNTMAX) GO TO 99
000054    TX(4)=XP
000055    TX(5)=FP
000056    T=TX(4)-TX(6)
000060    IF (T.EQ.0.) GO TO 99
000061    IF (ABS(FP).LT.TX(3)) GO TO 18
000063    R=TX(5)-TX(7)
000065    IF (R.EQ.0.) GO TO 99
000066    XP=TX(4)-TX(5)*(T/R)
000072    IF (TX(5)*TX(7).LT.0.) GO TO 11
000074    IF (TX(5)*TX(9).GE.0.) GO TO 11
000076    IF (XP.GT.TX(4)) GO TO 6
000102    IF (XP.GT.TX(8)) GO TO 10
000105    8 XP=TX(4)-TX(5)*(TX(4)-TX(8))/(TX(5)-TX(9))
000114    10 TX(7)=TX(5)
000116    TX(6)=TX(4)
C      GO GET F(XP)
000117    RETURN
000120    6 IF (XP.GT.TX(8)) GO TO 8

```

```
000124      GO TO 10
000124      11 TX(9)=TX(7)
000126      TX(8)=TX(6)
000127      GO TO 10
C HAVE FOUND A SOLUTION
000130      18 TX(10)=0.
000131      TX(1)=XP
000132      TX(4)=XP
000133      RETURN
C AN ERROR HAS OCCURED
C SET COUNT NEGATIVE AND EXIT
000134      99 TX(10)=-TX(10)
000136      RETURN
000136      END
```

## APPENDIX C

### THE GAMMA-LAW EQUATION OF STATE AND HUGONIOT TEMPERATURE PROGRAMS

The HOM equation of state used in FORTRAN SIN requires fits to the equation of state parameters for detonation products and condensed components. The FORTRAN BKW code<sup>8</sup> produces the coefficients to the required fits using the Becker-Kistiakowsky-Wilson equation of state to describe the isentrope of the detonation products.

In this appendix we describe a code which will produce the coefficients to the required fits using a gamma-law equation of state to describe the isentrope of the detonation products. We also describe a code which calculates the single-shock Hugoniot temperatures using the technique of Walsh and Christian<sup>9</sup> and produces the required fits for use in the FORTRAN SIN code.

#### The Gamma-Law Equation of State Program

##### A. The Nomenclature

|          |  |
|----------|--|
| CJ       | Chapman-Jouguet                                  |
| D        | detonation velocity                              |
| P        | pressure   |
| $U_p$    | particle velocity                                |
| V        | volume   |
| $V_o$    | initial specific volume                          |
| Z        | constant added to energies to make them positive |
| $\gamma$ | gamma  |
| $\rho_o$ | initial density                                  |

##### B. The Equations

$$P_{CJ} V_{CJ}^{\gamma} = C$$

$$V_{CJ} = \frac{\gamma V_o}{(\gamma + 1)}$$

$$\ln P = \ln C + \gamma \ln V$$

$$I = \frac{PV}{\gamma - 1} - \frac{P_{CJ} V_{CJ}}{\gamma - 1} + \frac{P_{CJ}}{2}(V_o - V_{CJ}) + Z$$

$$U_p = \frac{P_{CJ}}{\alpha' p D} \left[ 1 + \alpha' - \left( \frac{P}{P_{CJ}} \right)^{\alpha'} \right] \text{ where } \alpha' = \frac{\gamma - 1}{2\gamma}$$

$$\alpha = \left[ \left( \frac{(\alpha + 1)}{\left( 1 + \frac{d \ln D}{d \ln \rho} \right)} \right) - 2 \right]^{-1}$$

$$\beta = \frac{1 + \alpha}{\gamma}$$

##### C. The Input to the Code

| <u>Col.</u> | <u>Format</u> | <u>1st card</u>              |
|-------------|---------------|------------------------------|
| 1-72        | I2A6          | Alphabetic label for problem |
|             |               | <u>2nd card</u>              |
| <u>Col.</u> | <u>Format</u> |                              |
| 1-18        | E18.11        | $\gamma$                     |
| 19-36       | E18.11        | $P_{CJ}$ (Mbar)              |
| 37-54       | E18.11        | $\rho_o$ (g/cc)              |
|             |               | <u>3rd card</u>              |
| <u>Col.</u> | <u>Format</u> |                              |
| 1-18        | E18.11        | D                            |
| 19-36       | E18.11        | $d(\ln D)/d(\ln \rho)$       |
| 37-54       | E18.11        | Z                            |

##### D. The FORTRAN Code

```

      PROGRAM GLAW (INPUT,OUTPUT,FILM,TAPE12=FILM)
C      GAMMA,PCJ,RHO,DETV,DDDR,Z ARE INPUT CONSTANTS
000003      DIMENSION P(100),E(100),V(100),ALGP(100),ALGV(100),ALNE(100)
1,ALNP(100),UP(100),FTE(100),ECOEF(5),ALNV(100),W(100)
2,DELY(100),SB(5),T(5),A(5,5),LABEL(12),ST(5)
000003      DATA PLFACT/.0.8/
000003      DATA PMAX /+1.0/
000003      DATA PMIN /+1.0E-4/
000003      DATA PUFACT/+1.15/
000003      DATA AM /*0.4342944819/
000003      DATA ICHAR /044/
000003      DATA ICHAR2/063/
000003      500 READ 900,LABEL
000011      READ 901,GAMMA,PCJ,RHO
000023      READ 901,DETV,DDDR,Z
000035      900 FORMAT (12A6)
000035      901 FORMAT (4E18.11)
000035      FITR=-GAMMA
000037      ALPHA= 1.0/((GAMMA+1.)/(1.+DDDR) - 2.)
000045      BETA= (1+ALPHA)/GAMMA
000050      FITR= -1./BETA
000051      VCJ= GAMMA/((GAMMA+1.)*RHO)
000054      C = PCJ*(VCJ**GAMMA)
000060      ALNC= ALOG(C)
000062      ALPHP= (GAMMA -1.)/(2.*GAMMA)
000065      ENCT = -PCJ*VCJ/(GAMMA-1.) + 0.5*PCJ*(1./RHO -VCJ) + Z
000077      P(I)=PCJ
000100      I=1
000101      K=1
000102      DO 10 J = 1,100
000103      20 ALNP(I)=ALOG(P(I))
000107      ALGP(I)=ALNP(I)*AM
000111      ALNV(I)=-(ALNP(I)-ALNC)/ GAMMA
000115      ALGV(I)= ALNV(I)*AM
000117      V(I)=EXP(ALNV(I))
000122      E(I)=(P(I)*V(I))/(GAMMA-1.)*ENCT
000130      ALNE(I) = ALOG(E(I))
000134      IF(P(I).GT. PCJ) GO TO 12
000140      UP(I)= PCJ/(RHO* ALPHP*DETV)*(1.+ALPHP-(P(I)/PCJ)**ALPHP)
000152      P(I+1) =P(I)*PLFACT
000154      IF(P(I+1).LT. PMIN) GO TO 11
000156      I=I+1
000160      K=K+1
000161      GO TO 20
000161      11 P(I+1) = PCJ*PUFACT
000164      GO TO 13
000164      12 P(I+1)=P(I)*PUFACT
000167      13 IF(P(I+1).GT.PMAX) GO TO 30
000173      I=I+1
000174      GO TO 20
000174      10 CONTINUE
000176      30 CALL PFTS(I,4,0,SIGMA,ALNP,ALNE,W,FTE,DELY,ECOEF,SB,T,ST,A)
000214      PRINT 911,LABEL
000222      PRINT 902,GAMMA,PCJ,RHO
000234      PRINT 903,DETV,DDDR,Z
000246      PRINT 904,ALPHA,BETA,ENCT
000260      PRINT 905,FITR,C
000270      PRINT 906,ALNC,FITB
000300      PRINT 907,(ECOEF(I),I=1,5)
000312      PRINT 908
000316      NOH=I-K

```

```

000320      M= I
000321      DO 40 L = 1,NOH
000322      FTE(M)=EXP(FTE(M))
000326      PRINT 909,P(M),V(M),E(M),FTE(M)
000342      M=M-1
000344      40 CONTINUE
000346      DO 50 L = 1,K
000350      FTE(L)=EXP(FTE(L))
000354      PRINT 910,P(L),V(L),E(L),FTE(L),UP(L)
000372      50 CONTINUE
000375      WRITE (12,911) LABEL
000402      WRITE (12,902) GAMMA,PCJ,RHO
000414      WRITE (12,903) DETV,DDDR,Z
000426      WRITE (12,904) ALPHA,BETA,ENCT
000440      WRITE (12,905) FITR,C
000450      WRITE (12,906) ALNC,FITB
000460      WRITE (12,907) (ECOEF(I),I=1,5)
000472      WRITE (12,908)
000476      M=I
000500      DO 140 L = 1,NOH
000501      WRITE (12,909) P(M),V(M),E(M),FTE(M)
000514      M=M-1
000516      140 CONTINUE
000520      DO 150 L=1,K
000522      WRITE (12,910) P(L),V(L),E(L),FTE(L),UP(L)
000537      150 CONTINUE
C      GRAPH LOG PRESSURE VS VOLUME
000542      CALL ADV(1)
000543      CALL DGA (123.1023+0.900+-1.,+2.,+0.,,-4.)
000553      CALL DLGLG
000554      CALL SLLOG
000555      CALL SRLOG
000556      CALL PLOT (I,ALGV,1,ALGP,1,ICHAR,0)
000565      CALL PLOT (I,ALGV,1,ALGP,1,ICHAR2,0)
000574      CALL LINCNT (60)
000576      WRITE (12,900) LABEL
000604      WRITE (12,912)
C      GRAPH LOG PRESSURE VS PARTICLE VELOCITY
000610      CALL ADV(1)
000612      CALL DGA(123.1023,0,900+0.,+1.,+0.,,-4.)
000622      CALL DLNLG(10)
000624      CALL SLLOG
000625      CALL SHLIN(10,2)
000627      CALL PLOT (K,UP,1,ALGP,1,ICHAR,1)
000636      CALL LINCNT (60)
000640      WRITE (12,900) LABEL
000646      WRITE (12,913)
000652      GO TO 500
000653      911 FORMAT (27H1 GAMMA LAW CALCULATION FOR 12A6)
000653      902 FORMAT (/>.10H GAMMA IS ,1PE18.11,17H C-J PRESSURE IS ,1PE18.11,
112H DENSITY IS ,1PE18.11)
000653      903 FORMAT (/>.24H DETONATION VELOCITY IS .1PE18.11,18H DLND/DLN(RHO) IS
1S ,1PE18.11,31H Z-CONSTANT ADDED TO ENERGY IS ,1PE18.11)
000653      904 FORMAT (/>.19H COMPUTED ALPHA IS ,1PE18.11, 9H BETA IS ,1PE18.11,
123H ENERGY CONSTANT IS ,1PE18.11)
000653      905 FORMAT (/>.11H LNT = Q + ,1PE18.11,30H LNV AND PV TO GAMMA IS
1 ,1PE18.11)
000653      906 FORMAT (/>. 8H LN(P)= ,1PE18.11,3X,1PE18.11,5HLNV )
000653      907 FORMAT (/>.8H LN(E)= ,1PE18.11,3X,1PE18.11,5HLNP ,1PE18.11,6HLNP*2
1 ,1PE18.11,6HLNP*3 ,1PE18.11,5HLNP*4)
000653      908 FORMAT (/>.112H PRESSURE(MBARS) VOLUME (CC/GM) ENERGY
1 (MR-CC/GM) FIT ENERGY PARTICLE VELOCITY(CM/USEC))

```

```
000653    909 FORMAT(4(3X,1PE18.11))
000653    910 FORMAT(5(3X,1PE18.11))
000653    912 FORMAT (59H      THE PRESSURE-VOLUME ISENTROPE FOR GAMMA LAW ASSUMPT
                 ION )
000653    913 FORMAT (46H      THE PRESSURE -PARTICLE VELOCITY ISENTROPE )
000653        END
```

```

C          SUBROUTINE PFTS(M,KM,IW,SIGMA,X,F2,W,Y,DELY,B,SB,T,ST,A)
C          THIS IS A SPECIAL VERSION OF LA-PFTS FOR A MAX OF 100 POINTS
C          AND A MAX OF FIFTH DEGREE FIT NO PRINTING OR LEGENDRE POLYNOMIALS
C          ALSO WILL COMPUTE TILL GET THE FIT AND REQUIRES NO OUTPUT SUBROUTINE
C          M = NO OF DATA POINTS
C          KM = DEGREE OF FIT (MAX OF 5)
C          IW = 0 FOR NO WEIGHTS AND EQUAL 1 FOR WEIGHTS
C          SIGMA    IS STANDARD DEVIATION COMPUTED
C          X = X DATA INPUT ARRAY
C          F2 = F2 DATA ARRAY INPUT
C          W = WEIGHT DATA ARRAY INPUT SET EQUAL TO 1 IF IW IS 0
C          Y = F COMPUTED FROM FIT USING X
C          DELY = DIFFERENCE IN COMPUTED AND INPUT F
C          H = COEFFICIENTS TO FIT
C          SH = ESTIMATE OF ERRORS IN COEFFICIENTS TO FIT
C          T = COEFFICIENTS TO ORTHOGONAL POLYNOMINALS
C          ST = ERRORS IN T
C          A = AREA USED BY CALCULATION
000017      DIMENSION S(5),X(100),F2(100),ST(5),SB(5),F(100),PM(100),P(100)
1      * B(5),DELY(100),W(100),A(5,5),T(5),Y(100)
000017      LL=0
000020      9 FM=0.0
000021      A(1,1)=1.0
000024      A(2,2)=1.0
000026      FBAR=0.0
000027      XBAR=0.0
000030      D010I=1.M
000031      IF(IW)1009,1010,1009
000032      1010 w2=1.0
000034      w(I)=1.0
000037      GOTO1011
000040      1009 w2=SQRT(w(I))
000051      1011 FM=FM+W(I)
000055      F(I)=W2+F2(I)
000061      PM(I) = w2
000064      FBAR=FBAR+F(I)*PM(I)
000071      10 XBAR=XBAR+X(I)*PM(I)**2
000077      XBAR=XBAR/FM
000100      T(1)=FBAR/FM
000103      A(2,1)=-XBAR
000106      PXF=0.0
000107      PXP=0.0
000110      D020I=1.M
000111      P(I)=(X(I)-XBAR)*PM(I)
000117      PXF=PXF+P(I)*F(I)
000124      20 PXP=PXP+P(I)*P(I)
000131      T(2)=PXF/PXP
000134      PMXPM=FM
000136      S(1)=PMXPM
000137      KM=KM+1
000140      H(1)=T(1)*A(1,1)+T(2)*A(2,1)
000147      H(2)=T(2)*A(2,2)
000154      60 D0190K=2,KM
000156      IF(K-2)40,165,65
000160      40 STOP
000162      65 XXPXP=0.0
000163      XXPXPM=0.0
000164      H(K)=0.0
000167      D070J=1,M
000171      XP=X(J)*P(J)
000175      XXPXP=XXXPXP+XP*P(J)

```

```

000200      70 XPPXPM=XPPXPM+XP*PM(J)
000205      ALPHA=XPPXPM/PXP
000207      BETA=XPPXPM/PMXPM
000211      PPXF=0.0
000212      PPXPP=0.0
000213      D090I=1,M
000214      80 PT=P(I)
000217      81 P(I)=X(I)*PT-ALPHA*PT-BETA*PM(I)
000230      82 PPXF=PPXF+P(I)*F(I)
000235      83 PPXPP=PPXPP+P(I)*P(I)
000241      90 PM(I)=PT
000246      T(K)=PPXF/PPXPP
000252      PMXPM=PXP
000254      PXP=PPXPP
000254      A(K,1)=-ALPHA*A(K-1,1)-BETA*A(K-2,1)
000264      A(K,K-1)=A(K-1,K-2)-A(K-1,K-1)*ALPHA
000276      A(K,K)=1.0
000302      IF(K-3)150,150,110
000304      110 K1=K-2
000306      D0120I=2,K1
000310      120 A(K,I)=A(K-1,I-1)-ALPHA*A(K-1,I)-BETA*A(K-2,I)
000342      150 D0160I=1,K
000344      160 H(I)=H(I)+T(K)*A(K,I)
000364      165 SIG2=0.0
000365      D0180I=1,M
000367      Y(I)=POLY(X(I),K,H)
000404      175 DELY(I)=Y(I)-F2(I)
000413      180 SIG2=SIG2+(DELY(I)**2)*W(I)
000423      SIG2=SIG2/FLOAT(M-K)
000426      SIGMA=SQRT(SIG2)
000433      S(K)=PXP
000437      D0499I=1,K
000441      499 ST(I)=SIGMA/SQRT(S(I))
000457      D0501I=1,K
000461      SB(I)=0.0
000464      D0500J=1,K
000465      500 SB(I)=SB(I)+(A(J,I)*ST(J))**2
000507      501 SR(I)=SQRT(SB(I))
000522      190 CONTINUE
000524      220 KM=KM-1
000526      RETURN
000526      END

```

## The Hugoniot Temperature Program

### A. The Nomenclature

|              |   |
|--------------|---|
| $C$          | coefficients to $U_s = C + S(U_p)$ used             |
| $S$          | from $P_o$ to switch pressure                       |
| $C_1$        | coefficients to $U_s = C_1 + S_1(U_p)$ used         |
| $S_1$        | from switch pressure to maximum pressure            |
| $C_1$        | coefficients for electronic term                    |
| $C_{2o}$     | of Cowan equation of state                          |
| $(C_{3o})^2$ |   |
| $C_V$        | heat capacity (cal/g-°C)                            |
| $K$          | isothermal compressibility (Mbar <sup>-1</sup> )    |
| $P$          | pressure  |
| $T$          | temperature (°K)                                    |
| $T_o$        | initial temperature (°K)                            |
| $T_V$        | temperature (volts)                                 |
| $U_p$        | particle velocity                                   |
| $U_s$        | shock velocity                                      |
| $V_o$        | $1/n_o$   |
| $\alpha$     | linear coefficient of expansion (°C <sup>-1</sup> ) |
| $\Delta V$   | volume increment ( $\sim 1 \times 10^{-4}$ ) where  |
|              | $V_o - V_{\text{smallest}}/\Delta V < 5000$         |
| $\rho$       | density (g/cc)                                      |
| $\rho_o$     | initial density (g/cc)                              |

### B. The Equations

The following equation is solved

$$T = T_o e^{b(V_o - V)} + \frac{(V_o - V)P}{2C_V} + \frac{e^{-bV}}{2C_V} \times \int_{V_o}^V P e^{bV} [2 - b(V_o - V)] dV,$$

with

$$b = \frac{3\alpha}{K(C_V)}, \text{ using Simpson's rule.}$$

The input volume increment is used to compute a table of volumes which are used to compute pressures from

$$P = \frac{C^2(V_o - V)}{[V_o - S(V_o - V)]^2}.$$

The shock and particle velocities are found from

$$U_s = \frac{C + \sqrt{C^2 + 4SPV_o}}{2}$$

and

$$U_p = \frac{U_s - C}{S}.$$

The Cowan equation of state is

$$P = A + B\rho + C\rho^2 + D\rho^3 + E\rho^4 + (A_1 + A_2\rho)T_V + C_1 + \frac{(C_2\rho_o)}{\rho} + \frac{(C_3\rho_o)^2}{\rho^2} T_V^2,$$

where

$$\frac{3\alpha}{K} = A_1 + A_2\rho_o, \text{ and } A_2 = \frac{1.447404}{(\text{Atomic weight})},$$

which is the form used in FORTRAN HKW.<sup>8</sup>

### C. The Input to the Code

| <u>Col.</u> | <u>Format</u> | <u>1st card</u>              |
|-------------|---------------|------------------------------|
| 1-72        | 12A6          | Alphabetic label for problem |

| <u>Col.</u> | <u>Format</u> | <u>2nd card</u> |
|-------------|---------------|-----------------|
|-------------|---------------|-----------------|

|       |        |            |
|-------|--------|------------|
| 1-18  | E18.11 | $\alpha$   |
| 19-36 | E18.11 | $C_V$      |
| 37-54 | E18.11 | $T_o$      |
| 55-72 | E18.11 | $\Delta V$ |

| <u>Col.</u> | <u>Format</u> | <u>3rd card</u> |
|-------------|---------------|-----------------|
|-------------|---------------|-----------------|

|       |        |          |
|-------|--------|----------|
| 1-18  | E18.11 | $\rho_o$ |
| 19-36 | E18.11 | $K$      |
| 37-54 | E18.11 | $\rho$   |
| 55-72 | E18.11 |          |

| <u>Col.</u> | <u>Format</u> | <u>4th card</u> |
|-------------|---------------|-----------------|
|-------------|---------------|-----------------|

|       |        |                                |
|-------|--------|--------------------------------|
| 1-18  | E18.11 | Smallest P for temperature fit |
| 19-36 | E18.11 | Largest P for temperature fit  |

Note: If the two-phase feature is used, the temperature fit will include for the  $C_1$ ,  $S_1$  volumes only those temperatures which increase with decreasing volume.

| <u>Col.</u> | <u>Format</u> | <u>5th card</u> |
|-------------|---------------|-----------------|
|-------------|---------------|-----------------|

|       |        |                                   |
|-------|--------|-----------------------------------|
| 1-18  | E18.11 | Maximum pressure to be calculated |
| 19-36 | E18.11 | $C_1$                             |
| 37-54 | E18.11 | $S_1$                             |
| 55-72 | E18.11 | Switch pressure                   |

6th card

| Col.  | Format |                                       |
|-------|--------|---------------------------------------|
| 1-18  | E18.11 | Atomic weight. If zero, no Cowan fit. |
| 19-36 | E18.11 | $C_1$                                 |
| 37-54 | E18.11 | $C_{2p_0}$                            |
| 55-72 | E18.11 | $(C_{3p_0})^2$                        |

D. The FORTRAN Code

```

PROGRAM SEQ5 (INPUT,OUTPUT,FILM,TAPE12=FILM)
DIMENSION V(5011),P(5010),EP(5010),T(500),US(500),UP(500)
1,TC(5),FITT(500),LAREL(12),TV(500),ALNT(500),ALNVT(500)
2,TCALC(500),W(500),DELY(500),SB(5),TZ(5),A(5.5),PV(500),PP(500)
3,CRHO(500),ZP(500),CCOEF(5),ST(5),TX(10)

000003      DATA DKV /+11605.6/
000003      DATA CALMB /23890./
000003      DATA ICHAR /055/
000003      DATA TX(1) /0./
000003      DATA TX(2) /1.01/
000003      DATA TX(3) /+1.0E-5/
000003      DATA TX(10) /0./
000003
366 READ 900,LABFL
000011 READ 901,C,S,RHO,AK
000025 READ 901,ALPHA,CP,T0,DELTV
000041 READ 901,TP1,TP2
000051 READ 901,AMAXP,C1,S1,SWP
000065 READ 901,ATWT,AC1,AC2,AC3
C   C+S, C1,S1 COEFFICIENTS TO US-UP FITS
C   SWITCH FROM C,S TO C1,S1 AT SWP - THE SWITCH PRESSURE
C   ALPHA = LINEAR COEFFICIENT OF EXPANSION
C   CP    = HEAT CAPACITY IN CAL/GM/DEGC
C   AK    = ISOTHERMAL COMPRESSIBILITY IN MRARS
C   RHO   = DENSITY GM/CC
C   T0    = INITIAL TEMPERATURE IN DEG KELVIN
C   DETV  = VOLUME INCREMENT ABT 1 X 10-4
C   AMAXP = MAX PRESSURE
C   ATWT,AC1,AC2,AC3 COWAN EQ COEFFICIENTS SKIP IF ZERO
000101 V0=1./RHO
000103 Y=C
000105 Z=S
000106 I=?
000107 BCV=CP/CALMB
000111 B= 3.*ALPHA/(AK*BCV)
000114 V(2) = V0-DELTV
000116 SWV = 0.
000117 DO 10 J = 2,5000
000121 11 P(I)=(Y*Y*(V0-V(I)))/((V0-Z*(V0-V(I)))*(V0-Z*(V0-V(I))))
000132 IF(P(I).GT. AMAXP) GO TO 13
C   FOR PHASE CHANGE USE CONSTANT PRESSURE
000135 IF (P(I).LT.SWP.AND.Y.EQ.C1) P(I) = SWP
000147 IF (P(I).LT. SWP) GO TO 12
000152 Y=C1
000153 Z=S1
000155 IF (SWV.FQ.0.) SWV = V(I)
000157 12 EP(I)=P(I)*EXP(B*V(I))*(2.-B*(V0-V(I)))
000173 V(I+1) = V(I)-DELTV
000175 I = ?+1
000176 10 CONTINUE
000200 13 K=2
000201 M = I + 10
000203 DO 14 L = I,M
000204 P(L) = 0.
000205 14 CONTINUE
000207 I = I -1
000211 IT=1
000212 EP(1) = 0.
000213 PP(1) = 0.
000214 PV(1)= V0
000215 T(1)= T0
000217 US(1) = C

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000220      UP(1) = n.
000221      Y=C
000222      Z=S
000223      SUM = 1.
000224      DO 20 J=1,I,10
000225      21 PP(K)=P(J+10)
000230      IF (PP(K).LT.+1.E-8) GO TO 30
000232      PV(K)=V(J+10)
000234      IF (PV(K).GT.SWV) GO TO 27
000237      Y=C1
000240      Z=S1
000241      27 SUM = SUM + (EP(J)+4.*EP(J+1)+2.*EP(J+2)+ 4.*EP(J+3)
1.)+2.*FP(J+4)+4.*EP(J+5)+2.*EP(J+6)+4.*EP(J+7)+2.*EP(J+8)+24.*EP(J+9)+ FP(J+10)
000271      T(K)= T0*EXP(B*(VO-PV(K)))+ ((VO-PV(K))*PP(K))/(2.*BCV) -1*((EXP(-H*PV(K)))/(2.*BCV))*SUM*DELT/3.
000321      22 US(K)=(Y* SQRT(Y*Y + 4.*PP(K)*VO*Z))*0.5
000334      UP(K)=(US(K) -Y)/Z
000337      IF (T(K).LT.T(K-1)) GO TO 23
000341      IF (PP(K).GT.TP1.AND.PP(K).LT.TP2) GO TO 24
000351      GO TO 23
000351      24 ALNVT(IT)=ALOG(PV(K))
000355      ALNT (IT)=ALOG(T(K))
000361      IT=IT+1
000363      23 K=K+1
000365      20 CONTINUE
000367      30 IT =IT-1
000371      K=K-1
000372      HIP = PP(K)
000374      HIV = VO
000375      HIT = T(K)
000377      HIUS = US(K)
000400      HIUP = UP(K)
000402      CALL PFTS (IT,4.0,SIGMA,ALNVT,ALNT,W,TCALC,DELY,TC,SB,TZ,ST,A)
000417      PRINT 902,LABEL
000425      PRINT 903+C+S+SWP
000437      IF (SWP.GT.AMAXP) GO TO 41
000443      PRINT 904+SWP,AMAXP,C1+S1
000456      41 PRINT 905+RHO
000464      PRINT 906+AK
000472      PRINT 907+ALPHA
000500      PRINT 908+TO
000506      PRINT 909+CP
000514      PRINT 910+DEI,TV
000522      PRINT 911+TP1+TP2
000532      PRINT 912+ (TC(I),I=1,5)
000544      PRINT 913
000550      DO 42 I=1,K
000552      PRINT 914+ PV(I)+PP(I)+T(I)+US(I)+UP(I)
000567      42 CONTINUE
000572      PRINT 915
000575      DO 43 I=1,IT
000577      ALNVT(I)= EXP(ALNVT(I))
000603      ALNT(I)= EXP(ALNT(I))
000610      TCALC(I)=EXP(TCALC(I))
000615      PRINT 914, ALNVT(I), ALNT(I),TCALC(I)
000627
000632      43 CONTINUE
000637      WRITE(12,902) LABEL
000651      WRITE(12,903) C+S,SWP
000655      IF(SWP.GT.AMAXP) GO TO 51
000670      WRITE(12,904) SWP,AMAXP,C1+S1
51      WRITE(12,905) RHO

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000674      WRITE(12,906) AK
000704      WRITE(12,907) ALPHA
000712      WRITE(12,908) TO
000720      WRITE(12,909) CP
000726      WRITE(12,910) DELTV
000734      WRITE(12,911) TP1,TP2
000744      WRITE(12,912) (TC(I),I=1,5)
000756      WRITE(12,913)
000762      DO 52 I=1,K
000764      WRITE(12,914) PV(I),PP(I),T(I),US(I),UP(I)
001001      52 CONTINUE
001004      WRITE(12,915)
001007      DO 53 I=1,IT
001011      WRITE(12,914) ALNVT(I)+ALNT(I)+TCALC(I)
001022      53 CONTINUE
C      PRESSURE -VOLUME PLOT
001025      CALL ADV(1)
001026      CALL DGA(123,1023,0,900,0.,HIV,HIP,0.)
001036      CALL DLNLN (20,20)
001040      CALL SLLIN (20,2)
001042      CALL SBLIN (20,2)
001044      CALL PLOT (K,PV,1,PP,1,ICHAR,1)
001053      CALL LINCNT (60)
001055      WRITE (12,923)
001061      WRITE (12,900) LABEL
C      TEMPERATURE-VOLUME PLOT
001067      CALL ADV(1)
001071      CALL DLNLN (20,20)
001073      CALL DGA(123,1023,0,900,0.,HIV,HIT,0.)
001103      CALL SLLIN (20,1)
001105      CALL SBLIN (20,2)
001107      CALL PLOT (K,PV+1,T,1,ICHAR,1)
001116      CALL LINCNT (60)
001120      WRITE (12,924)
001124      WRITE (12,900) LABEL
C      PRESSURE-PARTICLE VELOCITY PLOT
001132      CALL ADV(1)
001134      CALL DGA(123,1023,0,900,0.,1,0,1.5,0.)
001144      CALL DLNLN (20,20)
001146      CALL SLLIN (20,2)
001150      CALL SBLIN (20,2)
001152      CALL PLOT (K,UP,1,PP,1,ICHAR,1)
001161      CALL LINCNT (60)
001163      WRITE (12,925)
001167      WRITE (12,900) LAHFL
C      SHOCK-PARTICLE VELOCITY PLOT
001175      CALL ADV(1)
001177      CALL DGA(123,1023,0,900,0.,HIUP,HTUS,0.)
001207      CALL DLNLN (20,20)
001211      CALL SLLIN (20,2)
001213      CALL SBLIN (20,2)
001215      CALL PLOT (K,UP,1,US,1,ICHAR,1)
001224      CALL LINCNT (60)
001226      WRITE (12,926)
001232      WRITE (12,900) LABEL
C      CALCULATE RESIDUAL TEMPERATURES
001240      600 TX(1) = V0
001242      DO 601 I = 1,K
001243      605 CALL LFR(VC,F,TX)
001246      IF (TX(1)) 602,603,604
001250      604 F = -VC + V0 + V0*3.4*ALPHA*(T(I)*EXP(B*(PV(I)-VC))-TO)
001265      GO TO 605

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C      USF US FOR RESIDUAL VOLUME AND UP FOR RESIDUAL TEMPERATURE
001265 603 US(I) = VC
001267 UP(I)=T(I) *EXP(B*(PV(I)-VC))
001276 601 CONTINUE
001300 GO TO 700
001301 602 PRINT 930
001305 GO TO 701
001306 700 PRINT 931
001312 PRINT 900,LABEL
001320 701 PRINT 932
001324 DO 702 I = 1,K
001326 PRINT 914,PV(I),PP(I),T(I),US(I),UP(I)
001343 702 CONTINUE
001346 WRITE (12,931)
001351 WRITE (12,900) LABEL
001357 WRITE (12,932)
001363 DO 703 I=1,K
001365 WRITE (12,914) PV(I),PP(I),T(I),US(I),UP(I)
001402 703 CONTINUE
001405 IF(ATWT.LT.0.1) GO TO 366
C      COWAN FIT
001407 100 DO 101 I=1,K
001411 TV(I)= T(I)/DKV
001413 CRHO(I)= 1./PV(I)
001415 101 CONTINUE
001417 A2=1.447404/ATWT
001421 A1=-A2*RH0 + 3.0*ALPHA*DKV/AK
001426 DO 102 I=1,K
001430 ZP(I)= PP(I)-(A1+A2*CRHO(I))*TV(I) -(AC1+AC2/CRHO(I)+AC3*AC3/
1(CRHO(I)*CRHO(I)))*TV(I)*TV(I)
001446 102 CONTINUE
001450 CALL PFTS (K,4,0,SIGMA,CRHO,ZP,W,FITT,DELY,CCOEF,SB,TZ,ST,A)
001466 PRINT 917
001472 PRINT 918,ATWT
001500 PRINT 919, (CCOEF(I),I=1,5)
001512 PRINT 920, A1,A2
001522 PRINT 921, AC1,AC2,AC3
001534 PRINT 922
001540 DO 103 I=1,K
001542 PRINT 914 ,ZP(I),FITT(I)
001551 103 CONTINUE
001554 WRITE (12,917)
001557 WRITE (12,918) ATWT
001565 WRITE (12,919) (CCOEF(I),I=1,5)
001577 WRITE (12,920) A1,A2
001607 WRITE (12,921) AC1,AC2,AC3
001621 WRITE (12,922)
001625 DO 104 I=1,K
001627 WRITE (12,914) ZP(I),FITT(I)
001636 104 CONTINUE
001641 GO TO 366
001641 900 FFORMAT (12A6)
001641 901 FORMAT (4E18.11)
001641 902 FORMAT (41H1 SOLID EQUATION OF STATE CALCULATION FOR,12A6)
001641 903 FORMAT (/, 6H US = ,1PE18.11,3H + ,1PE18.11,17H S FROM P0 TO ,
1PF18.11,10H MEGABARS )
001641 904 FORMAT (/, 6H FROM ,1PE18.11,13H MEGABARS TO ,1PF18.11,29H MEGABAR
1S USED THE FIT US = ,1PE18.11,3H + ,1PE18.11, 3H S )
001641 905 FORMAT (/,24H THE INITIAL DENSITY IS ,1PE18.11, 7H GM/CC )
001641 906 FORMAT (/,24H THE COMPRESSIBILITY IS ,1PE18.11)
001641 907 FORMAT (/,40H THE LINEAR COEFFICIENT OF EXPANSION IS ,1PE18.11)
001641 908 FORMAT (/,27H THE INITIAL TEMPERATURE IS,1PE18.11)

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001641      909 FORMAT (/,22H THE HEAT CAPACITY IS ,1PE18.11)
001641      910 FORMAT (/,25H THE VOLUME INCREMENT IS ,1PE18.11)
001641      911 FORMAT (/,32H THE TEMPERATURE FIT IS BETWEEN ,1PF18.11, 5H AND ,
11PF18.11,10H MEGABARS )
001641      912 FORMAT (/,8H LN(T)= ,1PE18.11,3X,1PE18.11,5H LNV ,1PE18.11,6H LNV*2
1 ,1PE18.11,6H LNV*3 ,1PE18.11,5H LNV*4)
001641      913 FORMAT (/,110H          VOLUME IN CC/GM           PRESSURE IN MEGABARS   TE
IMPERATURE DEG K     SHOCK VELOCITY           PARTICLE VELOCITY)
001641      914 FORMAT (5(4X,1PE18.11))
001641      915 FORMAT (   66H1          VOLUME IN CC/GM           INPUT TEMPERATURE   FI
1T TEMPERATURF )
001641      917 FORMAT (4I1H1 THE COWAN EQUATION OF STATE COEFFICIENTS )
001641      918 FORMAT (/,21H THE ATOMIC WEIGHT IS,1PE18.11)
001641      919 FORMAT (/,6H P = ,1PE18.11,3X,1PE18.11,5MRHO ,1PE18.11,6HRHO*2 ,
11PE18.11,6HRHO*3 ,1PE18.11,6HRHO*4 )
001641      920 FORMAT (/,5H ( ,1PE18.11,3X,1PE18.11,23H RHO ) TEMPERATURE )
001641      921 FORMAT (/,5H ( ,1PE18.11,3X,1PE18.11, 6H /RHO ,1PE18.11,24H/RHO*
12 )*TEMPERATURE*2 )
001641      922 FORMAT (/,40H          PRESSURE CALC         FIT PRESSURE )
001641      923 FORMAT (   40H PRESSURE-VOLUME HUGONIOT FOR   )
001641      924 FORMAT (   40H TEMPEPATURE- VOLUME HUGONIOT FOR   )
001641      925 FORMAT (   50H PRESSURE -PARTICLE VELOCITY HUGONIOT FOR   )
001641      926 FORMAT (   50H SHOCK VELOCITY-PARTICLE VELOCITY HUGONIOT FOR   )
001641      930 FORMAT(44H1 AN ERROR OCCURRED IN RESIDUAL TEMP CALC )
001641      931 FORMAT(44H1 RESIDUAL TEMPERATURE AND DENSITIES FOR   )
001641      932 FORMAT (/,114H          HUGONIOT VOLUME           HUGONIOT PRESSURE   HU
1GONIOT TEMPERATURE  RESIDUAL VOLUME           RESIDUAL TEMPERATURE )
001641      END

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SUBROUTINE LFR (XP,FP,TX)
C   TX(1)      INITIAL GUESS
C   TX(2)      RATIO TO GET SECOND POINT
C   TX(3)      ZERO DEFINITION
C   TX(10)     COUNT OF NUMBER OF ITRATIONS
C             SET TO ZERO ON SOLUTION
C             SET TO NEGATIVE OF COUNT ON ERROR
C   FP         =FUNCTION(XP)
C             WHEN A SOLUTION IS FOUND, XP IS THE ROOT
C
C             ERROR EXITS OCCUR FOR
C               1. TOO MANY ITERATIONS, .GT.CNTMAX
C               2. TWO SUCESSIVE XP'S OR FP'S ARE EQUAL
000005  DIMENSION TX(10)
000005  DATA CNTMAX /1000./
000005  IF (TX(10).LE.0.) GO TO 1
000006  TX(10)=TX(10)+1.
000011  IF (TX(10)-3.) 2,3,4
C   FNTRY FIPST TIME THROUGH
000014  1  IF (TX(1).EQ.0.) TX(1)=1.
000016  TX(10)=1.
000020  XP=TX(1)
C   GO GET F(XP)
000021  RETURN
C   ENTRY SECOND TIME THROUGH
000021  2 TX(9)=FP
000023  TX(8)=XP
000024  TX(5)=FP
000025  IF (ABS(FP).LT.TX(3)) GO TO 18
000027  XP=TX(1)+TX(2)
C   GO GET F(XP)
000030  RETURN
C   ENTRY THIRD TIME THROUGH
000031  3 TX(5)=FP
000033  TX(6)=XP
000034  TX(7)=FP
000035  IF (ABS(FP).LT.TX(3)) GO TO 18
000037  XP=TX(6)-TX(7)*(TX(6)-TX(8))/(TX(7)-TX(9))
C   GO GET F(XP)
000046  RETURN
C   ENTRY FOR FOURTH AND SUCCEEDING TIMES THROUGH
000047  4 IF (TX(10).GT.CNTMAX) GO TO 99
000053  TX(4)=XP
000054  TX(5)=FP
000055  T=TX(4)-TX(6)
000057  IF (T.EQ.0.) GO TO 99
000060  IF (ABS(FP).LT.TX(3)) GO TO 18
000062  R=TX(5)-TX(7)
000064  IF (R.EQ.0.) GO TO 99
000065  XP=TX(4)-TX(5)*(T/R)
000071  IF (TX(5)*TX(7).LT.0.) GO TO 11
000073  IF (TX(5)*TX(9).GE.0.) GO TO 11
000075  IF (XP.GT.TX(4)) GO TO 6
000101  IF (XP.GT.TX(8)) GO TO 10
000104  8 XP=TX(4)-TX(5)*(TX(4)-TX(8))/(TX(5)-TX(4))
000113  10 TX(7)=TX(5)
000115  TX(5)=TX(4)
C   GO GET F(XP)
000116  RETURN
000117  6 IF (XP.GT.TX(8)) GO TO 8
000123  GO TO 10

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```
000123      11 TX(9)=TX(7)
000125      TX(8)=TX(6)
000126      GO TO 10
000127      C HAVE FOUND A SOLUTION
000128      18 TX(10)=0.
000129      TX(1)=XP
000130      TX(4)=XP
000131      RETURN
000132      C AN ERROR HAS OCCURED
000133      C SET COUNT NEGATIVE AND EXIT
000134      99 TX(10)=-TX(10)
000135      RETURN
000136      END
```

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C      SUBROUTINE PFTS(M,KM,IW,SIGMA,X,F2,W,Y,DELY,B,SB,T,ST,A)
C      THIS IS A SPECIAL VERSION OF LA-PPTS FOR A MAX OF 500 POINTS
C      AND A MAX OF FIFTH DEGREE FIT NO PRINTING OR LEGENDRE POLYNOMIALS
C      ALSO WILL COMPUTE TILL GET THE FIT AND REQUIRES NO OUTPUT SUBROUTINE
C      M = NO OF DATA POINTS
C      KM = DEGREE OF FIT (MAX OF 5)
C      IW = 0 FOR NO WEIGHTS AND EQUAL 1 FOR WEIGHTS
C      SIGMA   IS STANDARD DEVIATION COMPUTED
C      X = X DATA INPUT ARRAY
C      F2 = F2 DATA ARRAY INPUT
C      W = WEIGHT DATA ARRAY INPUT SET EQUAL TO 1 IF IW IS 0
C      Y = F COMPUTED FROM FIT USING X
C      DELY = DIFFERENCE IN COMPUTED AND INPUT F
C      B = COEFFICIENTS TO FIT
C      SH = ESTIMATE OF ERRORS IN COEFFICIENTS TO FIT
C      T = COEFFICIENTS TO ORTHOGONAL POLYNOMINALS
C      ST = ERRORS IN T
C      A = AREA USED BY CALCULATION
000017  DIMENSION S(5),X(500),F2(500),ST(5),SB(5),F(500),PM(500),P(500)
1  +  B(5),DELY(500),W(500),A(5,5),T(5),Y(500)
000017
000020  LL=0
000021  9 FM=0.0
000021  A(1+1)=1.0
000024  A(2+2)=1.0
000026  FBAR=0.0
000027  XBAR=0.0
000030  D010I=1,M
000031  IF(IW)1009,1n10,1009
000032  1010 W2=1.0
000034  W(I)=1.0
000037  GOTOT0101
000040  1009 W2=SQRT(W(I))
000051  1011 FM=FM+W(T)
000055  F(I)=W2^4F2(I)
000061  PM(I) = W2
000064  FBAR=FRAR+F(I)*PM(I)
000071  1n  XBAR=XBAR+X(I)*PM(I)**2
000077  XBAR=XBAR/FM
000100  T(1)=FRAR/FM
000103  A(2+1)=-XBAR
000106  PXF=0.0
000107  PXP=0.0
000110  D020I=1,M
000111  P(I)=(X(I)-XBAR)*PM(I)
000117  PXF=PXF+D(I)*F(I)
000124  20 PXP=PXP+D(I)*P(I)
000131  T(2)=PXF/PXP
000134  PMXPM=FM
000136  S(1)=PMXPM
000137  KM=KM+1
000140  B(1)=T(1)*A(1,1)+T(2)*A(2,1)
000147  B(2)=T(2)*A(2,2)
000154  6n D019nK=2,KM
000155  IF(K-2)4n,165,65
000160  40 STOP
000162  65 XPXP=0.0
000163  XPM=0.0
000164  B(K)=0.0
000167  D070J=1,M
000171  XP=X(J)*P(J)
000175  XPXP=XPXP+XP*P(J)

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```

000200      70  XPXPM=XPXPM+XP*PM(J)
000205      ALPHA=XPXP/PXP
000207      BETA=XPXPM/PMXPM
000211      PPXF=0.0
000212      PPXPP=0.0
000213      DO90I=1,M
000214      80  PT=P(I)
000217      81  P(I)=X(I)*PT-ALPHA*PT-BETA*PM(I)
000230      82  PPXF=PPXF+P(I)*F(I)
000235      83  PPYPP=PPXPP+P(I)*P(I)
000241      90  PM(I)=PT
000246      T(K)=PPXF/PPYPP
000252      PMXPM=PXP
000254      PXP=PPXPP
000254      A(K,1)=-ALPHA*A(K-1,1)-BETA*A(K-2,1)
000264      A(K,K-1)=A(K-1,K-2)-A(K-1,K-1)*ALPHA
000277      A(K,K)=1.0
000303      IF(K=3)150,150,110
000305      110  K1=K-2
000307      DO120I=2,K1
000311      120  A(K,I)=A(K-1,I-1)-ALPHA*A(K-1,I)-BETA*A(K-2,I)
000344      150  DO160I=1,K
000346      160  B(I)=B(I)+T(K)*A(K,I)
000366      165  SIG2=0.0
000367      DO180I=1,M
000371      Y(I)=POLY(X(I),K,B)
000406      175  DELY(I)=Y(I)-F2(I)
000415      180  SIG2=SIG2+(DELY(I)**2)*W(I)
000426      SIG2=SIG2/FLOAT(M-K)
000430      SIGMA=SQRT(SIG2)
000436      S(K)=PXP
000442      DO499I=1,K
000444      499  ST(I)=SIGMA/SQRT(S(I))
000462      DO501I=1,K
000464      SB(I)=0.0
000467      DO500J=I,K
000470      500  SB(I)=SB(I)+(A(J,I)*ST(J))**2
000512      501  SR(I)=SQRT(SB(I))
000525      190  CONTINUE
000527      220  KM=KM-1
000531      RETURN
000531      END

```

```
000005      FUNCTION POLY  (X,N,A)
000005      DIMENSIONA(2)
000005      Y=A(N)
000007      DO1I=2,N
000010      J=N-I+1
000012      1 Y=A(J)+Y*X
000020      POLY =Y
000021      RETURN
000022      END
```

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